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The reports of research published in this magazine are necessarily qualified by the conditions of the tests from which the data are obtained Whenever it is deemed possible to do so, generalizations are drawn from the results of the tests; and, unless this is done, the conclusions formulated must be considered as specifically pertinent only to described conditions

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# STRENGTH TESTS OF CAST-IRON CULVERT PIPE 

Reported by E. F. KELLEY, Chief, Division of Tests, and W. F. KELLERMANN, Associate Materials Engineer, United States Bureau of Public Roads

THE SPECIFICATIONS for cast-iron culvert pipe which are in common use in highway work are greatly lacking in uniformity, and show a wide range in the requirements for strength and thickness of metal for pipe which presumably are to be subjected to similar conditions of service.

## inconsistencies found in specifications

Of 36 State highway department specifications current in 1931, 2 required a minimum strength in the 3 -edge bearing test but did not specify thickness of metal; 7 specified minimum thickness of metal but gave no strength requirements; and 27 specified both minimum strength and minimum shell thickness. In the specifications of the latter group the requirements for strength and shell thickness were not always consistent.

The minimum requirements for strength in the 3-edge bearing test ranged from 1,500 pounds per foot of diameter per linear foot of pipe $(1,500 \mathrm{D})$ to 3,000 pounds per foot of diameter per linear foot of pipe $(3,000 \mathrm{D})$. Fourteen States favored $1,500 \mathrm{D}$ for all sizes of pipe, 4 States specified $1,800 \mathrm{D}, 7$ States required $2,000 \mathrm{D}$ and 1 State required $3,000 \mathrm{D}$. Three States specified $1,500 D$ for pipe over 24 inches in diameter, and $2,000 \mathrm{D}$ for pipe under 24 inches in diameter.
The diversity of the requirements for minimum shell thickness of smooth or plain cast-iron pipe is shown graphically in figure 1. Thus the minimum thickness for 12 -inch pipe ranged from 0.31 to 0.54 inch and for 48 -inch pipe the range was from 0.75 to 1.38 inch, a difference of nearly 100 percent. The influence of the standard requirements for cast-iron water pipe are also shown in figure 1, 2 States having specified for culvert pipe the thicknesses required for class A water pipe in the sizes up to and including 36 -inch and 1 State specified the thickness required for the larger sizes of 42 inches and 48 inches.
The solid lines in figure 1 show the theoretical relationship between shell thickness and strength in the 3 -edge bearing test, for smooth cast-iron pipe without hubs, for an assumed modulus of rupture of 35,000 pounds per square inch. This modulus of rupture is an approximate average figure for modulus of rupture obtained in tests of sand-cast pipe. The dotted lines show the theoretical thicknesses increased by 10 percent, an allowance suggested to provide for unavoidable inaccuracy in manufacture. It is interesting to observe that the minimum thicknesses commonly specified for the smaller sizes of pipes were generally in excess of those which would be required for a load of $3,000 \mathrm{D}$ pounds per linear foot, while in the larger sizes the required thicknesses, in many cases, were below those which would be necessary to insure a load capacity of $2,000 \mathrm{D}$. It is believed that a strength of $2,000 D$ in the 3 -edge bearing test is the minimum which should be required for cast-iron pipe for use in culverts, yet 21 States, in 1931, specified a minimum shell thickness of 0.69 inch for 36 -inch pipe, which is too low to insure this strength in sand-cast pipe.

An example of the lack of relationship between requirements for strength and shell thickness was found in the specification of one State which required a minimum load of $1,500 \mathrm{D}$ for pipe having the thickness of class A water pipe. Pipe of this weight is generally more than adequate for a load of $3,000 \mathrm{D}$. Another State specification required a minimum strength of $3,000 \mathrm{D}$ but, for the larger sizes of pipe, specified minimum shell thicknesses insufficient for a load of $2,000 \mathrm{D}$.


Figure 1.-Relation Between Minimum Shell Thickness and Diameter of Smooth Cast-Iron Culvert Pipe as Specified by 34 States in 1931.

The testing of cast-iron culvert pipe to determine compliance with specification requirements for strength is an expensive procedure, particularly if the ultimate strength of the test specimens is determined, thereby destroying the pipe. With a sufficient knowledge of the strength characteristics of commercial cast-iron pipe, as influenced by shell thickness and diamater, it should be possible to eliminate much of this expense and to accept pipe on the basis of thickness and weight more generally than has been customary in the past. It was largely on this account that the tests described in this report were undertaken, but the data which have been developed should also prove useful in indicating revisions which might be made in existing specifications in the interest of uniformity and consistency.
The culvert pipe tested were as follows: ${ }^{1}$
Smooth, sand-cast pipe, furnished by one manufacturer in sizes from 12- to 48 -inch, and by another manufacturer in sizes from 12- to 36 -inch.

[^1]Smooth pipe cast by a centrifugal process in metal contact molds, in the sizes 12-, 16 -, and 20 -inch.

Spiral-corrugated pipe in sizes from 15 - to 36 -inch.
Ribbed pipe in the sizes $15-$, 18 -, and 24 -inch.
In general three specimens of each size and type were tested. Six specimens of each size of smooth sand-cast pipe and of smooth centrifugally cast pipe were supplied, 3 specimens had bells or hubs and 3 had plain ends. There were 6 specimens of each size of spiralcorrugated pipe, 3 specimens representing the pipe section and 3 representing the cuff section. All specimens had a net length of approximately 3 feet, exclusive of the overlapping portion of end fittings. Some had been cast in this length and the others were cut from longer pipe. The smooth pipe with plain ends were cut from pipe which had been cast with hubs.

The spiral-corrugated pipe had a relatively thin shell which was cast in the form of spiral circumferential corrugations. Sections of pipe are fastened together by screwing one into the other. Since each section of pipe is of uniform diameter, the inner, or pipe section, is of slightly smaller diameter than the outer or cuff section.
respect to the position of the point or center of load application, for pipes with bell ends, that the various standard and tentative standard specifications differ and this is important since the position of the load has a considerable influence on the ultimate strength developed in the test.

Three positions of the load are used in various specifications:
(a) Load at the center of the upper bearing block.
(b) Load at the center of the laying-length of the pipe. The laying-length of pipe is the distance from the spigot end to the inside shoulder of the bell and therefore is a length intermediate between the length of the upper bearing block and the full length of the pipe, including the bell.
(c) Load at the center of the length of the pipe as shown at the top of figure 3. This position results in less eccentricity of load application than the other two and is required by the most recent specifications. This position of load, with a few exceptions which will be mentioned later, was used in these tests.

Position (a) is required by the A.S.T.M. (American Society for Testing Materials) Standard Specifications


Figure 2.-Representative Specimens of Types of Pipe Tested. Specimens Are (Left to Right) Smooth Sand-Cast Pipe, Plain End; Smooth Sand-Cast Pipe, Bell End; Smooth Centrifugally Cast Pipe, Bell End; Ribbed Pipe; SpiralCorrugated Pipe.

The ribbed pipe had a relatively thin shell reinforced by four longitudinal ribs, and by transverse ribs, the spacing of which varied somewhat with the size of the pipe.

Representative specimens of the different types of pipe are illustrated in figure 2.

## SPECIFICATIONS VARY AS TO POSITION OF LOAD

All pipe were tested for strength in the 3 -edge bearing test. This test has been used on sewer pipe and culvert pipe for a number of years and has become an accepted standard but it has not been completely standardized in one important respect. This is frequently overlooked and merits some discussion.

The general set-up for the test is shown in figure 3. The lower bearing consists of a rigid block to which are securely fastened two longitudinal wooden strips having vertical sides with the interior top corners rounded to a radius of approximately one half inch. The earlier specifications required that these strips be spaced 1 inch apart while the more recent ones provide that the space between them shall be not less than one half inch or more than 1 inch for each foot of nominal pipe diameter. The upper bearing, through which the load is applied, is a rigid wooden block. In the case of pipe with plain ends the upper and lower bearings extend the full length of the pipe while for pipe with bell ends the bearings extend from the spigot end to the point where the barrel begins to flare out to meet the bell. It is with
for Clay Sewer Pipe, C13-24 and A.S.T.M. Standard Specifications for Cement-Concrete Sewer Pipe, C14-24.

Position (b) is required by the 1926 Tentative Standard Specifications for Reinforced Concrete Culvert Pipe of the Joint Concrete Culvert Pipe Committee and by the Tentative Standard Methods of Sampling and Testing Highway Materials of the American Association of State Highway Officials as published in United States Department of Agriculture Bulletin No. 1216. Both of these have since been revised but the latter is still used to some extent.

Position (c) is required by the 1928 Tentative Standard Specifications of the Joint Concrete Culvert Pipe Committee; by the A.S.T.M. Tentative Standard Specifications for Reinforced-Concrete Culvert Pipe, C76-30T, which, in substance, are the same as the 1928 specifications of the Joint Committee; by the A.S.T.M. Tentative Standard Specifications for ReinforcedConcrete Pipe, C75-30T; and by the 1931 edition of the Tentative Standard Specifications for Highway Materials and Methods of Sampling and Testing of the American Association of State Highway Officials, which is a revision of Department of Agriculture Bulletin No. 1216.

The State specifications for making strength tests, discussed above, referred variously to A.S.T.M. Specifications C13-24 and C14-24 and to Bulletin No. 1216 of the Department of Agriculture. Some specified the 3 -edge bearing test without describing it, others gave


3-EDGE BEARINGS FOR PIPE WITH BELL END


3-EDGE BEARINGS FOR PIPE WITHOUT BELL END
Figure 3.-Position of Bearings in Cast-iron Pipe Tests.
incomplete descriptions which did not define the position of load, another fairly large group required the test for strength to be made "in the manner prescribed by Committee C-4, American Society for Testing Materials." The latter is a particularly ambiguous requirement since, prior to 1932, all of the A.S.T.M. specifications to which reference has been made were under the jurisdiction of Committee C-4 and that, in addition to the 3 -edge bearing test, these specifications also recognize the 2 -edge bearing test and the sandbearing test.

In conducting the 3 -edge bearing test on the specimens included in this investigation, the distance between the longitudinal strips of the lower bearing was varied as shown in the following table:

| Size of <br> pipe | Distance <br> between <br> strips |
| :---: | :---: |
|  | Inches |
| 12 | Inches |
| 15 | 1 |
| 16 | 1 |
| 18 | 1 |
| 20 | 1 |
| 24 | 2 |
| 30 | 2 |
| 36 | 3 |
| 42 | 3 |
| 48 | 3 |
|  |  |

The test load was applied to the upper bearing block at the center of the length of the pipe with the exception of four specimens of 12 -inch pipe with bell ends. Three of these were sand-cast pipe furnished by manufacturer A and one was a specimen of centrifugally cast pipe (tables 1 and 3). In the case of the exceptions


Figure 4.-Forty-Eight-Inch Pipe Set up in 200,000-Pound Testing Machine.
mentioned, the load was applied at the center of the length of bearing block and therefore was eccentric with respect to the center of length of the pipe.

## TESTING APPARATUS DESCRIBED

Since a machine designed particularly for pipe testing was not available, the 3 -edge bearing tests were made in a 200,000 -pound universal testing machine having two extensions, or wings, attached to opposite sides and forming a part of the weighing table. The general arrangement of the testing apparatus is shown in figure 4. The cover page shows a 48 -inch plain-end pipe ready for testing. The pipe was placed on one extension of the weighing table and on the opposite extension there was placed a vertical steel member of suitable height which served as a support for the loading beam and also as a counter weight. Two I-beams extending across the weighing table were supported on one side by a knifeedge bearing block on top of the vertical steel member and on the other side by a roller bearing which rested on the upper bearing block on the pipe. The load was applied through an eyebar and pin, the pin being supported by the I-beams at mid-span between the two bearings and the eyebar extending down through the movable head of the testing machine. A nut and washer on the lower end of the eyebar made contact with the movable head as it was lowered and thus transmitted load to the two bearings of the I-beams. With this arrangement the test load on the pipe was one half the load indicated on the weighing beam of the testing machine. During application of the load, the testing machine was run in low gear which corresponded to an idle crosshead speed of 0.05 inch per minute.

Straight bearing blocks of the same type were used on all types of pipe. This resulted in a much smaller area of contact on the special types of pipe than on the smooth pipe. On the corrugated pipe the applied load was concentrated on the upper surfaces of the corrugations and on the ribbed pipe the load was concentrated on the transverse ribs, the specimens being arranged for the test so that no load was applied to the longitudinal ribs. Figure 5 shows specimens of the corrugated pipe and the ribbed pipe with the bearing blocks which were used in testing them.

As has been stated, in general three specimens of each size and type of pipe were tested. On one pipe of each group of three, vertical deflections were measured during the loading tests with micrometer dials reading to 0.001 inch. Two such dials were used, one at each

Table 1.-Smooth pipe, sand-cast, manufacturer A, S-edge bearing, load applied at center of pipe unless otherwise noted ${ }^{1}$

| Type | Identification no. | Nomi- nal size | Weight | Thickness at break ${ }^{2}$ |  | Laying length | Length of bearing | Load at failure |  | orting ngth, inds oot of eter oot of length | Kemarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plain end | SP-12-1 | $\begin{array}{r} \text { Inches } \\ 12 \\ 12 \\ 12 \end{array}$ | $\begin{array}{\|c} \text { Pounds } \\ 172 \\ 170 \\ 170 \end{array}$ | Inches $\begin{array}{r} 0.45 \\ .44 \\ .44 \end{array}$ | Inches $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{gathered} \text { Inches } \\ 36 \\ 36 \\ 36 \end{gathered}$ | Inches $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | Pounds $\begin{aligned} & 25,550 \\ & 23,250 \\ & 22,950 \end{aligned}$ | $\begin{aligned} & 8,520 \\ & 7,750 \\ & 7,650 \end{aligned}$ | Average 7,970 | - |
| Bell end. | SB-12-1 ${ }^{2}$ | $\begin{aligned} & 12 \\ & 12 \\ & 12 \end{aligned}$ | $\begin{aligned} & 190 \\ & 190 \\ & 192 \end{aligned}$ | $\begin{array}{r} .49 \\ .42 \\ .46 \end{array}$ | $\begin{aligned} & 381 / 2 \\ & 381 / 2 \\ & 381 / 2 \end{aligned}$ | $\begin{aligned} & 35^{3} \\ & 35^{3} \\ & 35^{3} / 4 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 18,750 \\ & 18,950 \\ & 18,950 \end{aligned}$ | 6, 290 6, 360 6, 360 | 6, 340 | Load applied at center of bearing. Do. <br> Do. |
| Plain end | SP-16-1 ${ }^{\text {S }}$ | $\begin{aligned} & 16 \\ & 16 \\ & 16 \end{aligned}$ | $\begin{aligned} & 256 \\ & 250 \\ & 252 \end{aligned}$ | $\begin{aligned} & .55 \\ & .50 \\ & .51 \end{aligned}$ | $\begin{aligned} & 35^{3 / 4} \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35^{3} / 4 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 353 / 4 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 24,250 \\ & 22,050 \\ & 22,310 \end{aligned}$ | $\begin{aligned} & 6,100 \\ & 5,510 \\ & 5,580 \end{aligned}$ | 5, 730 |  |
| Bell end. | SB-16-1 ${ }^{\text {S }}$ [ ${ }^{\text {S }}$ | $\begin{aligned} & 16 \\ & 16 \\ & 16 \end{aligned}$ | $\begin{aligned} & 300 \\ & 296 \\ & 304 \end{aligned}$ | $\begin{aligned} & .54 \\ & .52 \\ & .55 \end{aligned}$ | $\begin{aligned} & 381 / 4 \\ & 381 / 2 \\ & 381 / 4 \end{aligned}$ | $\begin{aligned} & 351 / 2 \\ & 351 / 2 \\ & 353 / 4 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 25,450 \\ & 24,200 \\ & 27,300 \end{aligned}$ | $\begin{aligned} & 6,450 \\ & 6,140 \\ & 6,870 \end{aligned}$ | 6, 490 | Broke through the bell. |
| Plain end. | SP-20-1 ${ }^{\text {S }}$ | $\begin{aligned} & 20 \\ & 20 \\ & 20 \end{aligned}$ | $\begin{aligned} & 346 \\ & 346 \\ & 314 \end{aligned}$ | $\begin{array}{r} .53 \\ .50 \\ .50 \end{array}$ | $\begin{aligned} & 361 / 4 \\ & 35^{3} / 4 \\ & 36 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 35^{3} 3 \\ & 36 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 35^{3} / 4 \\ & 36 \end{aligned}$ | $\begin{aligned} & 21,950 \\ & 19,500 \\ & 16,750 \end{aligned}$ | $\begin{aligned} & 4,360 \\ & 3,930 \\ & 3,350 \end{aligned}$ | 3, 880 |  |
| Bell end | SB-20-1 ${ }^{\text {S }}$ | $\begin{aligned} & 20 \\ & 20 \\ & 20 \end{aligned}$ | $\begin{aligned} & 404 \\ & 376 \\ & 406 \end{aligned}$ | $\begin{array}{r} .54 \\ .50 \\ .58 \end{array}$ | $\begin{aligned} & 381 / 2 \\ & 381 / 2 \\ & 381 / 2 \end{aligned}$ | $\begin{aligned} & 35^{3 / 4} \\ & 35^{3 / 4} \\ & 36 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 25,600 \\ & 19,250 \\ & 27,050 \end{aligned}$ | $\begin{aligned} & 5,150 \\ & 3,870 \\ & 5,410 \end{aligned}$ | 4,810 | Do. <br> Do. |
| Plain end | SP-24-1 ${ }^{\text {P }}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 416 \\ & 432 \\ & 424 \end{aligned}$ | $\begin{array}{r} .54 \\ .56 \\ .55 \end{array}$ | $\begin{aligned} & 353 / 4 \\ & 353 \\ & 35 \frac{3}{4} \end{aligned}$ | $\begin{aligned} & 35^{3} 3 \\ & 35^{3} \\ & 353 \\ & 3 \end{aligned}$ | $\begin{aligned} & 35^{3} / 4 \\ & 35^{3} \\ & 353 \\ & 35 \end{aligned}$ | $\begin{aligned} & 14,300 \\ & 18,000 \\ & 19,600 \end{aligned}$ | $\begin{aligned} & 2,400 \\ & 3,020 \\ & 3,290 \end{aligned}$ | 2,900 | Crack in one side before test. |
| Bell end. | SB-24-1 ${ }^{\text {P }}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 540 \\ & 532 \\ & 538 \end{aligned}$ | $\begin{aligned} & .60 \\ & .57 \\ & .58 \end{aligned}$ | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 35^{3} 3 \\ & 35^{3} 3 \\ & 35^{3} / 4 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 25,850 \\ & 23,500 \\ & 21,850 \end{aligned}$ | $\begin{aligned} & 4,340 \\ & 3,940 \\ & 3,670 \end{aligned}$ | 3,980 |  |
| Plain end. | SP-30-1 ${ }^{\text {S }}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 644 \\ & 662 \\ & 646 \end{aligned}$ | $\begin{aligned} & .68 \\ & .74 \\ & .73 \end{aligned}$ | $\begin{aligned} & 353 / 4 \\ & 353 / 4 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35^{3} / 4 \\ & 35^{3 / 4} \\ & 36 \end{aligned}$ | $\begin{aligned} & 35^{3} \\ & 35^{3 / 4} \\ & 36 \end{aligned}$ | 22,300 21,200 <br> 20,500 | $\begin{aligned} & 2,990 \\ & 2,850 \\ & 2,730 \end{aligned}$ | 2, 860 |  |
| Bell end | SB-30-1 ${ }^{\text {S }}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 770 \\ & 768 \\ & 784 \end{aligned}$ | .79 .73 .75 | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 35^{3} 3 \\ & 35^{3} / 4 \\ & 36 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 26,300 \\ & 22,900 \\ & 25,250 \end{aligned}$ | $\begin{aligned} & 3,530 \\ & 3,070 \\ & 3,370 \end{aligned}$ | 3, 320 | Broke through the bell. Do. Do. |
| Plain end | SP-36-1 ${ }^{\text {S }}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{array}{r} 882 \\ 886 \\ 1,000 \end{array}$ | $\begin{array}{r} .84 \\ .79 \\ .91 \end{array}$ | $\begin{aligned} & 35^{3} / 4 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35^{3} / 4 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35^{3 / 4} \\ & 36 \\ & 36 \end{aligned}$ | 25, 400 <br> 16, 450 <br> 28, 500 | $\begin{aligned} & 2,840 \\ & 1,830 \\ & 3,170 \end{aligned}$ | 3, 000 | Flaw in one end of break. Not included in average. |
| Bell end | $\begin{array}{r} \mathrm{SB}-36-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 1,070 \\ & 1,086 \\ & 1,052 \end{aligned}$ | .87 .85 .82 | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 35^{3} / 4 \\ & 35^{3} 4 \\ & 35^{3} 4 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | 26, 850 <br> 31, 600 <br> 30, 850 | $\begin{aligned} & 3,000 \\ & 3,530 \\ & 3,450 \end{aligned}$ | 3,330 | Broke through the bell. Do. <br> Do. |
| Plain end. | $\begin{array}{r} \mathrm{SP}-42-1 \\ 2 \\ 3 \end{array}$ | 42 42 42 | 1,300 1,340 1,230 | $\begin{array}{r} 1.06 \\ 1.00 \\ .93 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ |  | $\begin{aligned} & 3,420 \\ & 2,980 \\ & 2,950 \end{aligned}$ | 3, 120 |  |
| Bell end. | $\begin{array}{r} \text { SB-42-1 } \\ 2 \\ 3 \end{array}$ | 42 42 42 | 1,520 1,470 1,540 | $\begin{array}{r} 1.00 \\ .92 \\ 1.02 \end{array}$ | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 39,900 \\ & 36,550 \\ & 38,500 \end{aligned}$ | $\begin{aligned} & 3,800 \\ & 3,480 \\ & 3,670 \end{aligned}$ | 3, 650 | $\begin{aligned} & \text { Do. } \\ & \text { Do. } \\ & \text { Do. } \end{aligned}$ |
| Plain end. | $\begin{array}{r} \text { SP- } 48-1 \\ 2 \\ 3 \end{array}$ | 48 48 48 | 1,400 1,420 1,400 | $\begin{array}{r} 1.02 \\ .90 \\ .97 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 25,200 \\ & 22.300 \\ & 23,450 \end{aligned}$ | $\begin{aligned} & 2,100 \\ & 1,860 \\ & 1,950 \end{aligned}$ | 1,970 |  |
| Bell end. | $\begin{array}{r} \text { SB- } 48-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 48 \\ & 48 \\ & 48 \end{aligned}$ | $\begin{aligned} & 1,695 \\ & 1,712 \\ & 1,680 \end{aligned}$ | $\begin{array}{r} 1.00 \\ 1.03 \\ .92 \end{array}$ | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 31,950 \\ & 29,350 \\ & 24,850 \end{aligned}$ | $\begin{aligned} & 2,660 \\ & 2,450 \\ & 2,070 \end{aligned}$ | 2, 390 | $\begin{aligned} & \text { Do. } \\ & \text { Do. } \\ & \text { Do. } \end{aligned}$ |

Lower bearing blocks 1 inch apart for 12 - and 16 -inch pipe; 2 inches for 20 -, 24 -, and 30 -inch pipe; 3 inches for 36 -, 42 -, and 48 -inch pipe.
Plain-end pipe-thickness is average of measurements at 10 points equally spaced along the crack. Bell-end pipe-thickness of barrel at spigot end.
end of the pipe. They were set 1 inch in from the ends of the pipe except when the specimens had bell ends, in which case the dial at the bell end was set 1 inch in from the inside shoulder of the bell. Figure 6 shows the position of the dials as they were set to measure the deflections of smooth pipe with plain ends. Deflections were observed for increments of load up to maximum values of from 10,000 to 15,000 pounds, after which the readings were discontinued. The results of the 3 -edge bearing tests are shown in tables 1 to 5 , inclusive.
These tables show the principal dimensions of each pipe tested and the load at failure. As a basis for comparison they also show the "supporting strength" in pounds per foot of diameter per foot of laying length. This supporting strength was determined by dividing the applied load by the product of the internal diameter and the laying length (in feet) and is hereafter referred to as the "strength."

## LOCATION OF CRACK AT FAILURE AN INDICATION OF UNIFORMITY

When an elastic ring is supported along the bottom element and a concentrated load is applied along the top element, as in the 2-edge bearing test, the maximum positive bending moments in the ring occur at the top and bottom, directly under the load and directly over the support. The bending moment in the ring decreases from a maximum positive value at the crown to a maximum negative value at the horizontal axis, passing through zero at a point the radius to which makes an angle with the vertical of approximately $40^{\circ} .^{2}$ The maximum positive bending moment at the crown is about 75 percent greater than the maximum negative moment at the horizontal axis.

In the 3 -edge bearing test, as conducted on cast-iron pipe of ordinary dimensions, the bending moments are

[^2] Bulletin No. 22, University of Illinois.

Table 2.-Smooth pipe, sand-cast, manufacturer B, S-edge bearing, load applied at center of pipe ${ }^{1}$

| Type | Identification no. | $\begin{gathered} \text { Nominal } \\ \text { size } \end{gathered}$ | Weight | Thickness at break ${ }^{2}$ | Over-all length | Laying length | Length of bearing | Load at failure | Supportin pounds diameter laying | strength, foot of per foot of ength | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plain end | $\begin{array}{r} \mathrm{SP}-12-1 \\ 2 \\ 3 \end{array}$ | Inches $\begin{aligned} & 12 \\ & 12 \\ & 12 \end{aligned}$ | $\begin{array}{r} \text { Pounds } \\ 172 \\ 161 \\ 164 \end{array}$ | Inches $\begin{array}{r} 0.51 \\ .46 \\ .48 \end{array}$ | Inches $\begin{aligned} & 36 \\ & 36 \end{aligned}$ $36$ | $\begin{array}{r} \text { Inches } \\ 36 \\ 36 \\ 36 \end{array}$ | Inches $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{array}{r} \text { Pounds } \\ 24,600 \\ 20,700 \\ 25,950 \end{array}$ | $\begin{aligned} & 8,200 \\ & 6,900 \\ & 8,650 \end{aligned}$ | $\begin{array}{r} \text { Average } \\ 7,920 \end{array}$ |  |
| Bell end. | $\begin{array}{r} \text { SB-12-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 12 \\ & 12 \\ & 12 \end{aligned}$ | $\begin{aligned} & 185 \\ & 183 \\ & 183 \end{aligned}$ | $\begin{array}{r} .50 \\ .42 \\ .50 \end{array}$ | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 361 / 4 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 351 / 2 \\ & 351 / 2 \\ & 351 / 2 \end{aligned}$ | $\begin{aligned} & 29,150 \\ & 26,350 \\ & 28,500 \end{aligned}$ | $\begin{aligned} & 9,650 \\ & 8,720 \\ & 9,430 \end{aligned}$ | 9,270 | Broke through the bell. Do. <br> Do. |
| Plain end | $\begin{array}{r} \text { SP-18-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 18 \\ & 18 \\ & 18 \end{aligned}$ | $\begin{aligned} & 226 \\ & 225 \\ & 235 \end{aligned}$ | $\begin{array}{r} .48 \\ .44 \\ .47 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 12,850 \\ & 14,600 \\ & 18,350 \end{aligned}$ | $\begin{aligned} & 2,860 \\ & 3,240 \\ & 4,080 \end{aligned}$ | 3,390 |  |
| Bell end. | $\begin{array}{r} \text { SB-18-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 18 \\ & 18 \\ & 18 \end{aligned}$ | $\begin{aligned} & 275 \\ & 277 \\ & 276 \end{aligned}$ | $\begin{array}{r} .45 \\ .43 \\ .50 \end{array}$ | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 21,050 \\ & 14,750 \\ & 17,350 \end{aligned}$ | $\begin{aligned} & 4,680 \\ & 3,280 \\ & 3,860 \end{aligned}$ | 3,940 |  |
| Plain end. | SP-24-1 | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 405 \\ & 434 \\ & 406 \end{aligned}$ | $\begin{array}{r} .60 \\ .62 \\ .60 \end{array}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 17,050 \\ & 21,300 \\ & 20,100 \end{aligned}$ | $\begin{aligned} & 2,920 \\ & 3,650 \\ & 3,450 \end{aligned}$ | 3,340 |  |
| Bell end. | SB-24-1 ${ }^{\text {S }}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 474 \\ & 471 \\ & 464 \end{aligned}$ | .62 .60 .56 | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 19,950 \\ & 19,800 \\ & 19,650 \end{aligned}$ | $\begin{aligned} & 3,320 \\ & 3,300 \\ & 3,280 \end{aligned}$ | 3,300 | $\begin{aligned} & \text { Do. } \\ & \text { Do. } \\ & \text { Do. } \end{aligned}$ |
| Plain end | $\begin{array}{r} \mathrm{SP}-30-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 582 \\ & 574 \\ & 587 \end{aligned}$ | .70 .68 .68 | $\begin{aligned} & 343 / 4 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 343 / 4 \\ & 35 \\ & 35 \end{aligned}$ | $343 / 4$ 35 35 | 19, 650 <br> 19, 350 <br> 17, 750 | $\begin{aligned} & 2,710 \\ & 2,650 \\ & 2,430 \end{aligned}$ | 2,600 |  |
| Bell end. | $\begin{array}{r} \text { SB- } 30-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 652 \\ & 665 \\ & 654 \end{aligned}$ | .62 .50 .64 | 39 39 39 | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 35 \\ & 35 \\ & 35 \end{aligned}$ | $\begin{aligned} & 21,650 \\ & 16,000 \\ & 19,350 \end{aligned}$ | $\begin{aligned} & 2,890 \\ & 2,130 \\ & 2,580 \end{aligned}$ | 2,530 | Do. |
| Plain end. | $\begin{array}{r} \text { SP- } 36-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{array}{r} 3940 \\ 3940 \\ 3940 \end{array}$ | .95 .94 .91 | $\begin{aligned} & 341 / 2 \\ & 341 / 2 \\ & 341 / 2 \end{aligned}$ | $\begin{aligned} & 341 / 2 \\ & 341 / 2 \\ & 341 / 2 \end{aligned}$ | $\begin{aligned} & 341 / 2 \\ & 341 / 2 \\ & 341 / 2 \end{aligned}$ | $\begin{aligned} & 30,450 \\ & 29,250 \\ & 23,550 \end{aligned}$ | $\begin{array}{r} 3,530 \\ 3,390 \\ 42,730 \end{array}$ | 3,460 |  |
| Bell end. | SB-36-1 2 | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 3 \\ 3 \\ 3 \\ 3 \end{array} 1,100 \\ & { }^{3} 1,100 \end{aligned}$ | .92 .95 .92 | $\begin{aligned} & 39 \\ & 39 \\ & 39 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 341 / 2 \\ & 341 / 2 \\ & 341 / 2 \end{aligned}$ | $\begin{aligned} & 37,550 \\ & 32,100 \\ & 34,950 \end{aligned}$ | $\begin{aligned} & 4,170 \\ & 3,570 \\ & 3,880 \end{aligned}$ | 3,870 | $\begin{aligned} & \text { Do. } \\ & \text { Do. } \\ & \text { Do. } \end{aligned}$ |

${ }^{1}$ Lower bearing blocks 1 inch apart for 12 - and 18 -inch pipe; 2 inches for 24 - and 30 -inch pipe; 3 inches for 36 -inch pipe.
2 Plain-end pipe-thickness is average of measurements at 10 points equally spaced along the crack. Bell-end pipe-thickness of barrel at spigot end.
${ }^{3}$ Approximate.
${ }_{4}$ Cracked before test, not included in average.
Table 3.-Smooth pipe, centrifugally-cast, 3-edge bearing, load applied at center of pipe unless otherwise noted ${ }^{1}$

| Type | Identification no. | $\underset{\text { Nize }}{\text { Nominal }}$ | Weight | Thickness at break ${ }^{2}$ | Over-all length | Laying length | Length of bearing | Load at failure | Support pound diamet of layi | strength, per foot of per foot length | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plain end | $\begin{array}{r} \text { CP-12-1 } \\ 2 \\ 3 \end{array}$ | Inches 12 12 12 | $\begin{array}{r} \text { Pounds } \\ 165 \\ 168 \\ 166 \end{array}$ | Inches $\begin{array}{r} 0.42 \\ .41 \\ .42 \end{array}$ | Inches 36 36 36 | $\begin{array}{r} \text { Inches } \\ 36 \\ 36 \\ 36 \end{array}$ | Inches $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | Pounds $\begin{aligned} & 25,950 \\ & 27,050 \end{aligned}$ $27,800$ | $\begin{aligned} & 8,650 \\ & 9,020 \\ & 9,270 \end{aligned}$ | $\begin{aligned} & \text { Average } \\ & 8,980 \end{aligned}$ |  |
| Bell end | $\begin{array}{r} \text { CB-12-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 12 \\ & 12 \\ & 12 \end{aligned}$ | $\begin{aligned} & 246 \\ & 250 \\ & 246 \end{aligned}$ | $\begin{array}{r} .44 \\ .43 \\ .43 \end{array}$ | $\begin{aligned} & 403 / 4 \\ & 41 \\ & 401 / 2 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 37 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 34 \\ & 34 \\ & 30 \end{aligned}$ | $\begin{aligned} & 31,475 \\ & 34,650 \\ & 24,700 \end{aligned}$ | $\begin{array}{r} 10,420 \\ 11,230 \\ 8,180 \end{array}$ | 10,820 | Load applied at center of bearing. Not included in average. |
| Plain end | $\begin{array}{r} \mathrm{CP}-16-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 16 \\ & 16 \\ & 16 \end{aligned}$ | $\begin{aligned} & 278 \\ & 280 \\ & 282 \end{aligned}$ | $\begin{array}{r} .51 \\ .49 \\ .58 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36^{1 / 4} \end{aligned}$ | $\begin{aligned} & 32,300 \\ & 32,400 \\ & 39,650 \end{aligned}$ | $\begin{aligned} & 8,080 \\ & 8,100 \\ & 9,840 \end{aligned}$ | 8,670 |  |
| Bell end. | $\begin{array}{r} \text { CB- } 16-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 16 \\ & 16 \\ & 16 \end{aligned}$ | $\begin{aligned} & 404 \\ & 400 \\ & 402 \end{aligned}$ | $\begin{aligned} & .51 \\ & .51 \\ & .51 \end{aligned}$ | $\begin{aligned} & 401 / 2 \\ & 401 / 2 \\ & 40^{3} / 4 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 33 \\ & 33 \\ & 33 \end{aligned}$ | $\begin{aligned} & 38,000 \\ & 40,950 \\ & 40,460 \end{aligned}$ | $\begin{array}{r} 9,500 \\ 10,240 \\ 10,040 \end{array}$ | 9,930 |  |
| Plain end. | $\begin{array}{r} \text { CP-20-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 20 \\ & 20 \\ & 20 \end{aligned}$ | $\begin{aligned} & 452 \\ & 440 \\ & 446 \end{aligned}$ | $\begin{array}{r} .63 \\ .65 \\ .59 \end{array}$ | $\begin{aligned} & 361 / 4 \\ & 361 / 2 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 361 / 2 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 361 / 2 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 32,350 \\ & 37,950 \\ & 33,100 \end{aligned}$ | $\begin{aligned} & 6,430 \\ & 7,490 \\ & 6,570 \end{aligned}$ | 6,830 |  |
| Bell end. | $\begin{array}{r} \mathrm{CB}-20-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 20 \\ & 20 \\ & 20 \end{aligned}$ | $\begin{aligned} & 570 \\ & 572 \\ & 580 \end{aligned}$ | $\begin{array}{r} .64 \\ .60 \\ .66 \end{array}$ | $\begin{aligned} & 401 / 2 \\ & 41 \\ & 41 \end{aligned}$ | $\begin{aligned} & 361 / 4 \\ & 361 / 2 \\ & 361 / 4 \end{aligned}$ | $\begin{aligned} & 33 \\ & 33 \\ & 33 \end{aligned}$ | 44, 500 40, 950 45, 250 | $\begin{aligned} & 8,840 \\ & 8,080 \\ & 8,990 \end{aligned}$ | 8,640 |  |

${ }_{1}$ Lower bearing blocks 1 inch apart for 12 - and 16 -inch pipe; 2 inches apart for 20 -inch pipe.
${ }^{2}$ Plain-end pipe-thickness is average of measurements at 10 points equally spaced along the crack. Bell-end pipe-thickness of barrel at spigot end.
substantially the same as in the 2 -edge test. In the 3 -edge test, as will be shown later, the moment at the crown is less than in the 2 -edge test by an insignificant amount. Also in the 3-edge test the moment at the bottom of the pipe is slightly less than at the top.

Therefore, it is to be expected that a pipe which is exactly circular and of uniform thickness will crack, under the ultimate load in the 3 -edge bearing test, along the upper element. Failure of the crack to develop in this position is evidence of nonuniformity,
either in cross section or quality of metal. A slight nonuniformity may cause the pipe to break at the bottom rather than at the top but a crack along the horizontal axis evidences nonuniformity of considerable magnitude.
About 80 percent of the specimens of smooth sandcast pipe furnished by manufacturer A broke at the top and the remainder broke at the bottom except one specimen which broke at a flaw near the bottom. Of the smooth sand-cast pipe of manufacturer B, one

Table 4.-Spiral-corrugated pipe, 3-edge bearing, load applied at center of pipe ${ }^{1}$

| Type | Identification no. | $\underset{\text { size }}{\text { Nominal }}$ | Weight | Thickness at break | Over-all length | Laying length | Length of bearing | Load at first crack | Load at failure | Supporting strength, pounds per foot of diameter per foot of laying length- |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  | At first crack | Average | At failure | Average |
| Pipe | $\begin{array}{r} \mathrm{M}-15-1 \\ 2 \\ 3 \end{array}$ | Inches $\begin{aligned} & 15 \\ & 15 \\ & 15 \end{aligned}$ | $\begin{array}{r} \text { Pounds } \\ 152 \\ 151 \\ 152 \end{array}$ | Inches $0.27-0.27$ $.30-.30$ $.28-.28$ | Inches $383 / 4$ $383 / 4$ $383 / 4$ | Inches $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | Inches $3833^{3}$ 3834 3834 | $\begin{array}{r} \text { Pounds } \\ 12,700 \\ 14,600 \\ 15,050 \end{array}$ | $\begin{array}{r} \text { Pounds } \\ 15,450 \\ 15,000 \\ 15,050 \end{array}$ | $\begin{aligned} & 3,390 \\ & 3,890 \\ & 4,010 \end{aligned}$ | 3, 760 | $\begin{aligned} & 4,120 \\ & 4,000 \\ & 4,010 \end{aligned}$ | 4, 040 |
| Cuff | $\begin{array}{r} \mathrm{F}-15-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 15 \\ & 15 \\ & 15 \end{aligned}$ | $\begin{aligned} & 157 \\ & 153 \\ & 160 \end{aligned}$ | $\begin{aligned} & .24-.33 \\ & .22-.32 \\ & .24-.37 \end{aligned}$ | $\begin{aligned} & 3834 \\ & 3834 \\ & 3834 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 3833^{3} \\ & 3834 \\ & 383 / 4 \end{aligned}$ | $\begin{array}{r} 12,900 \\ 13,150 \\ 9,050 \end{array}$ | $\begin{aligned} & 12,900 \\ & 14,700 \\ & 13,200 \end{aligned}$ | $\begin{aligned} & 3,440 \\ & 3,510 \\ & 2,410 \end{aligned}$ | 3,120 | $\begin{aligned} & 3,440 \\ & 3,920 \\ & 3,520 \end{aligned}$ | 3,630 |
| Pipe | $\begin{array}{r} \mathrm{M}-18-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 18 \\ & 18 \\ & 18 \end{aligned}$ | $\begin{aligned} & 177 \\ & 169 \\ & 168 \end{aligned}$ | $\begin{aligned} & .26-.26 \\ & .28-.29 \\ & .24-.28 \end{aligned}$ | $\begin{aligned} & 383 / 4 \\ & 39 \\ & 383 / 4 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 383 / 4 \\ & 39 \\ & 383 / 4 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 1,250 \\ 12,500 \\ 11,800 \end{array} \end{aligned}$ | $\begin{aligned} & 14,250 \\ & 13,400 \\ & 12,650 \end{aligned}$ | $\begin{aligned} & 3,170 \\ & 2,780 \\ & 2,520 \end{aligned}$ | 2,860 | $\begin{aligned} & 3,170 \\ & 2,980 \\ & 2,810 \end{aligned}$ | 2,990 |
| Cuff | $\begin{array}{r} \text { F-18-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 18 \\ & 18 \\ & 18 \end{aligned}$ | $\begin{aligned} & 192 \\ & 187 \\ & 190 \end{aligned}$ | $\begin{aligned} & .20-.30 \\ & .25-.34 \\ & .22-.30 \end{aligned}$ | $\begin{aligned} & 383 / 4 \\ & 3834 \\ & 383 / 4 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 38^{3 / 4} \\ & 38^{3 / 4} \\ & 388^{3}, 4 \end{aligned}$ | $\begin{aligned} & 12,950 \\ & 12,000 \\ & 11,250 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 12,950 \\ 12,600 \\ 11,900 \end{array} \end{aligned}$ | $\begin{aligned} & 2,880 \\ & 2,670 \\ & 2,500 \end{aligned}$ | 2,680 | $\begin{aligned} & 2,880 \\ & 2,800 \\ & 2,640 \end{aligned}$ | 2,770 |
| Pipe | $\begin{array}{r} \mathrm{M}-24-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 286 \\ & 285 \\ & 286 \end{aligned}$ | $\begin{aligned} & .33-.33 \\ & .32-.32 \\ & .32-.32 \end{aligned}$ | $\begin{aligned} & 391 / 2 \\ & 391 / 2 \\ & 391 / 2 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 391612 \\ & 3912 \\ & 3912 \end{aligned}$ | $\begin{aligned} & 15,800 \\ & 11,300 \\ & 13,050 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 5,800 \\ 12,700 \\ 13,150 \end{array} \end{aligned}$ | $\begin{aligned} & 2,630 \\ & 1,880 \\ & 2,170 \end{aligned}$ | 2,230 | $\begin{aligned} & 2,630 \\ & 2,120 \\ & 2,190 \end{aligned}$ | 2,310 |
| Cuff | $\begin{array}{r} \text { F-24-1 } \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 285 \\ & 289 \\ & 291 \end{aligned}$ | $\begin{aligned} & .32-.33 \\ & .35-.40 \\ & .33-.36 \end{aligned}$ | $\begin{aligned} & 3915 \\ & 391 / 2 \\ & 391 / 2 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 39112 \\ & 3916 \\ & 3912 \end{aligned}$ | $\begin{aligned} & 12,100 \\ & 15,250 \\ & 15,000 \end{aligned}$ | $\begin{aligned} & 12,30 \\ & 15,400 \\ & 15,000 \end{aligned}$ | $\begin{aligned} & 2,020 \\ & 2,540 \\ & 2,500 \end{aligned}$ | 2,350 | $\begin{aligned} & 2,050 \\ & 2,570 \\ & 2,500 \end{aligned}$ | 2,370 |
| Pipe | $\begin{array}{r} \mathrm{M}-30-1 \\ 2 \\ 2 \end{array}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & \begin{array}{l} 421 \\ 420 \\ 425 \end{array} \end{aligned}$ | $\begin{array}{r} .38-.43 \\ .34-.39 \\ .38-.38 \end{array}$ | $\begin{aligned} & 391 / 2 \\ & 391 / 2 \\ & 391 / 2 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 3916 \\ & 3916 \\ & 3915 \end{aligned}$ | $\begin{aligned} & 17,350 \\ & 20,250 \\ & 22,400 \end{aligned}$ | $\begin{aligned} & 20,650 \\ & 21,700 \\ & 23,050 \end{aligned}$ | $\begin{aligned} & 2,310 \\ & 2,700 \\ & 2,990 \end{aligned}$ | 2,670 | $\begin{aligned} & 2,750 \\ & 2,890 \\ & 3,070 \end{aligned}$ | 2,900 |
| Cuff | $\begin{array}{r} \mathrm{F}-30-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 30 \\ & 30 \\ & 30 \end{aligned}$ | $\begin{aligned} & 467 \\ & 481 \\ & 480 \end{aligned}$ | $\begin{aligned} & .45-.55 \\ & .37-.49 \\ & .35-.45 \end{aligned}$ | $\begin{aligned} & 3916 \\ & 391 / 2 \\ & 3916 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 391,2 \\ & 391 / 2 \\ & 3912 \end{aligned}$ | $\begin{aligned} & 21,550 \\ & 19,950 \\ & 19,500 \end{aligned}$ | $\begin{array}{r} 22,450 \\ 20,950 \\ 21,800 \end{array}$ | $\begin{aligned} & 2,870 \\ & 2,660 \\ & 2,600 \end{aligned}$ | 2, 710 | $\begin{aligned} & 2,990 \\ & 2,790 \\ & 2,910 \end{aligned}$ | 2,900 |
| Pipe. | $\begin{array}{r} \mathrm{M}-36-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 557 \\ & 560 \\ & 557 \end{aligned}$ | $\begin{array}{r} .43-.45 \\ .42-.43 \\ .43-.44 \end{array}$ | $\begin{aligned} & 4014 \\ & 40 y_{4} \\ & 40 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 401 / 4 \\ & 401 / 4 \\ & 40 \end{aligned}$ | $\begin{aligned} & 21,400 \\ & 19,150 \\ & 20,400 \end{aligned}$ | $\begin{aligned} & 21,800 \\ & 22,000 \\ & 21,700 \end{aligned}$ | $\begin{aligned} & 2,380 \\ & 2,130 \\ & 2,270 \end{aligned}$ | 2, 260 | $\begin{aligned} & 2,420 \\ & 2,440 \\ & 2,410 \end{aligned}$ | 2,420 |
| Cuff | $\begin{array}{r} \mathrm{F}-36-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 646 \\ & 636 \\ & 631 \end{aligned}$ | $\begin{aligned} & .45-.57 \\ & .41-.56 \\ & .45-.57 \end{aligned}$ | $\begin{aligned} & 40 \\ & 401 / 4 \\ & 40 \end{aligned}$ | 36 36 36 | $\begin{aligned} & 40 \\ & 401 / 4 \\ & 40 \end{aligned}$ | $\begin{aligned} & 24,300 \\ & 23,400 \\ & 25,000 \end{aligned}$ | $\begin{aligned} & 26,600 \\ & 27,000 \\ & 25,500 \end{aligned}$ | $\begin{aligned} & 2,700 \\ & 2,600 \\ & 2,780 \end{aligned}$ | 2,690 | $\begin{aligned} & 2,960 \\ & 3,000 \\ & 2,830 \end{aligned}$ | 2,930 |

${ }^{1}$ Lower bearing blocks 1 inch apart for 15 - and 18 -inch pipe; 2 inches for 24 - and 30 -inch pipe; 3 inches for 36 -inch pipe.
2 Thickness at break taken under load at end of pipe which cracked first. First value-thickness at bottom of corrugation. Second value-thickness at top of corrugation.
Table 5.-Ribbed pipe, S-edge bearing, load applied at center of pipe ${ }^{1}$

| Type | Identifi-eationno. | $\underset{\text { size }}{\text { Nominal }}$ | Weight | Thickness at break ${ }^{2}$ | Distance from bell end to center line of first transverse rib | Distance between transverse ribs | Number of transverse ribs | Overall length | Laying length | Load at first crack | Load at failure | Supporting strength, pounds per foot of diameter per foot of laying length- |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  | At first crack | Average | At failure | A verage |
| Bell end. | $\begin{array}{r} \mathrm{R}-15-1 \\ 2 \end{array}$ | $\begin{aligned} & \text { Inches } \\ & 15 \\ & 15 \end{aligned}$ | $\begin{array}{r} \text { Pounds } \\ 150 \\ 150 \end{array}$ | $\begin{gathered} \text { Inches } \\ 0.24-0.79 \\ .33-.91 \end{gathered}$ | $\begin{gathered} \text { Inches } \\ 57 / 8 \\ 57 / 8 \end{gathered}$ | Inches 678 678 | 5 | $\begin{gathered} \text { Inches } \\ 36 \\ 36 \end{gathered}$ | $\begin{gathered} \text { Inches } \\ 341 / 2 \\ 3412 \end{gathered}$ | $\begin{array}{r} \text { Pounds } \\ 9,850 \\ 11,250 \end{array}$ | $\begin{array}{r} \text { Pounds } \\ 11,100 \\ 12,900 \end{array}$ | $\begin{aligned} & 2,740 \\ & 3,130 \end{aligned}$ | 2, 940 | $\begin{aligned} & 3,090 \\ & 3,590 \end{aligned}$ | 3,340 |
| Do. | $\begin{array}{r} \mathrm{R}-18-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 18 \\ & 18 \\ & 18 \end{aligned}$ | $\begin{aligned} & 230 \\ & 228 \\ & 228 \end{aligned}$ | $\begin{aligned} & .30-1.05 \\ & .28-1.03 \\ & .28-1.00 \end{aligned}$ | $\begin{aligned} & 55, \\ & 558 \\ & 5 \% \end{aligned}$ | $\begin{aligned} & 6116 \\ & 6116 \\ & 61 / 16 \end{aligned}$ | 6 6 6 | $\begin{aligned} & 3816 \\ & 381 / 2 \\ & 381 / 2 \end{aligned}$ | $\begin{aligned} & 37 \\ & 37 \\ & 37 \end{aligned}$ | $\begin{aligned} & 19,000 \\ & 19,650 \\ & 17,000 \end{aligned}$ | $\begin{aligned} & 22,650 \\ & 19,650 \\ & 21,450 \end{aligned}$ | $\begin{aligned} & 4,110 \\ & 4,250 \\ & 3,680 \end{aligned}$ | 4, 010 | $\begin{aligned} & 4,900 \\ & 4,250 \\ & 4,640 \end{aligned}$ | 4, 600 |
| Do. | $\begin{array}{r} \mathrm{R}-24-1 \\ 2 \\ 3 \end{array}$ | $\begin{aligned} & 24 \\ & 24 \\ & 24 \end{aligned}$ | $\begin{aligned} & 310 \\ & 306 \\ & 303 \end{aligned}$ | $\begin{aligned} & .25-1.20 \\ & .33-1.20 \\ & .30-1.16 \end{aligned}$ | $\begin{aligned} & 615 / 2 \\ & 61 / 2 \\ & 61 / 2 \end{aligned}$ | $\begin{aligned} & 73 / 6 \\ & 73166 \\ & 73 / 6 \end{aligned}$ | 5 5 5 | $\begin{aligned} & 371 / 2 \\ & 371 / 2 \\ & 371 / 2 \end{aligned}$ | $\begin{aligned} & 36 \\ & 36 \\ & 36 \end{aligned}$ | $\begin{aligned} & 13,300 \\ & 14,850 \\ & 14,200 \end{aligned}$ | $\begin{aligned} & 15,000 \\ & 18,550 \\ & 17,000 \end{aligned}$ | $\begin{aligned} & 2,220 \\ & 2,470 \\ & 2,370 \end{aligned}$ | 2,350 | $\begin{aligned} & 2,500 \\ & 3,090 \\ & 2,830 \end{aligned}$ | 2,810 |

${ }^{1}$ Lower bearing blocks 1 inch apart for 15 - and 18 -inch pipe; 2 inches for 24 -inch pipe.
${ }^{2}$ First value - thickness of barrel at spigot end. Second value-total thickness of barrel and rib at first rib from spigot end.
third broke at the top and one third broke either at the bottom, or at the top and bottom approximately simultaneously. The remainder, except two in which the exact location of the crack was not determined, broke either at the side, or at the top and side, bottom and side, or top, bottom and side, simultaneously. About 65 percent of the specimens of spiral corrugated pipe broke at the top and the remainder, except three specimens in which the exact location of the crack was not determined, broke at the bottom. All specimens of the smooth, centrifugally cast pipe broke along the top indicating a greater uniformity in this group than in the other three which have been discussed. This is probably due to the method of manufacture which
may be expected to result in a more uniform thickness of metal than sand-casting methods.

Ribbed pipe of the type tested is not of uniform cross section, and failure of the shell will not necessarily occur at the top. The bending moment on the horizontal axis through the center of the ring produces tensile stress in the outer fibers and the tensile stress produced in the small rib sections may be sufficient to produce initial failure at this point even though the bending moment is much less than at the crown, where the ribs are in compression. This type of failure actually occurred as was evidenced by crack development during the tests and by the fact that all of the eight specimens tested broke along both sides. Five of


Figure 5.-Ribbed Pipe and Spiral-Corrugated Pipe with Bearing Blocks Used in 3-Edge Bearing Test.
them also broke at the top and one of these five also broke at the bottom.
In testing the smooth pipe with bell ends it was observed in numerous cases that, at failure, a crack developed in the body of the pipe without the development of a visible crack in the bell. The other cases, in which the crack developed throughout the length of the specimen, are indicated in tables 1 and 2.

## INFLUENCE OF POSITION OF LOAD SHOWN IN TEST RESULTS

The test results for 12 -inch pipe shown in tables 1 and 3 show that the position of the center of load application on the upper bearing block has an important influence on the strength developed by pipe with bell ends in the 3 -edge bearing test. The tests of 12 -inch pipe with bell ends reported in table 1 were all with the load applied at the center of the bearing block. The center of the load was 15 inches from the spigot end and the eccentricity of load, with respect to the center of length of the pipe, was $4 \frac{1}{4}$ inches. The average strength of the bell-end pipe ( $6,340 \mathrm{D}$ ) was only 80 percent of the average strength of the 12 -inch pipe with plain ends $(7,970 \mathrm{D})$ on which the load was applied at the center of the pipe. In all the other tests of bell-end pipe shown in table 1 the load was applied at the center of the pipe and in every case the average strength of the bell-end pipe was greater than the average strength of plain-end pipe of corresponding size.

Bell-end pipe CB-12-3 (table 3) was tested with the point of load application at the center of the bearing block, the eccentricity with respect to the center of the pipe being $5 \frac{1}{4}$ inches. The strength of this pipe was only 76 percent of the average strength of specimens CB-12-1 and CB-12-2 which were tested with the load in the center of the pipe. Also, the strength was only 91 percent of the average strength of the 12 -inch pipe with plain ends. As in table 1, the average strength of all other bell-end pipe in table 3 is greater than the
average strength of plain-end pipe of corresponding size. The influence of the position of the point of load application is also shown by the deflection measurements which will be discussed later.
It is apparent that the application of load at the center of the bearing block rather than at the center of length of the pipe subjects pipe with bell ends to an unduly severe load condition which results in an apparent lowering of their strength in the 3-edge bearing test. That it is not a fair test is evidenced by the failure of pipe loaded in this manner under lower loads than for failure of plain-end pipe of similar dimensions.

STRENGTH TESTS DISCUSSED
The average strength of bell-end specimens of the smooth, sand-cast pipe of manufacturer A (table 1),


Figure 6.-Position of Micrometer Dials for Measuring Deflections of Smooth Pipe with Plain Ends.

Table 6.-Vertical deflections of pipe

and the smooth, centrifugally cast pipe (table 3) which were loaded at the center of length was greater in all cases than the average strength of the corresponding specimens with plain ends. However, this was not always true of individual specimens.

For example: Bell-end pipe SB-20-2 developed a lower strength than the corresponding plain-end pipes SP-20-1 and SP-20-2; pipe SB-36-1 was not as strong as the plain-end specimen SP-36-3; and specimen SB-48-3 showed a lower strength than specimen SP-48-1. In the centrifugally cast pipe, bell-end specimen CB-16-1 developed a lower strength than the corresponding plain-end specimen CP-16-3. These apparent discrepancies may be attributed partly to differences in quality of metal and partly to differences in shell thickness due to unavoidable inaccuracies in manufacture.

In the smooth, sand-cast pipe of manufacturer B (table 2) the effect of the bell ends on strength is less pronounced than in the pipe of manufacturer A and the centrifugally cast pipe. This is probably due to differences in the design of the bells. (See fig. 7 for
typical cross sections of 12 -inch pipe.) There are more cases in which individual specimens with bell ends developed less strength than specimens of the same size with plain ends. In the case of the 24 - and 30 -inch pipe, even the average strength of the bell-end pipe was somewhat less than that of the pipe with plain ends.
Pipe with bell ends normally may be expected to develop a greater strength in the 3 -edge bearing test, with the load applied at the center of length of the pipe, than pipe of the same size and dimensions with plain ends. However, these tests have shown that this differential in strength cannot always be expected on account of inaccuracy in manufacture and differences in quality of metal. It is indicated also that the amount of any strength differential which exists is influenced by the design of the bell. It is reasonable to assume that the differential is also dependent on the length of the specimen, being less for long pipe than for short ones. Since culvert pipe is furnished in lengths up to 12 feet, and it has been found in these tests that the 3 -foot


Figure 7.-Sections of Bell-End Pipe, Nominal Diameter 12 Inches.
specimens with bell ends did not consistently show a higher strength than pipe with plain ends, it is concluded that the design of cast-iron pipe to withstand the 3 -edge bearing test may more safely be based on the results of tests on plain-end specimens than on tests of bell-end specimens.
In the tests of spiral corrugated pipe (table 4) and ribbed pipe (table 5) it was observed that the specimens cracked at a load which was generally, but not always, somewhat less than the ultimate load. Both the load at which the first crack developed and the ultimate load are reported although the former is considered to be more significant of the ability of the pipe to withstand the strength test.
The average strength at first crack of all sizes of corrugated pipe and ribbed pipe exceeded 2,000 pounds per foot of diameter per foot of length and only one specimen (M-24-2) developed a strength lower than this.
The supporting strength of spiral corrugated pipe is so dependent on the dimensions of the corrugations and that of ribbed pipe is so dependent on the size and location of the ribs that no general conclusions may be drawn from the results of these tests. The strengths reported are those developed by pipe of certain dimensions and design and it is not possible to derive from these results data applicable to pipe of different design or dimensions. The only conclusion which appears to be justified is that corrugated or ribbed pipe, similar in all respects to those included in these tests, may be expected to develop a strength in the 3 -edge bearing test of at least $2,000 \mathrm{D}$ pounds per linear foot of laying length.

## deflection of Pipe discussed

Typical load-deflection curves obtained in these tests are shown in figure 8. The curves for all the other specimens are of the same general character varying only in the magnitude and relationship of deflections at a given load.
The significant data with respect to vertical deflections are given in table 6. This table shows the deflections of all specimens under a load of 3,000 pounds per foot of laying length, the maximum load at which readings on all pipe were available. For comparison, a second set of deflections under a different load is also given. For the smooth sand-cast and centrifugally cast pipe this load is 4,000 pounds per foot of laying length and for the spiral-corrugated and ribbed pipe it is 2,000 pounds per foot of laying length.

The smooth sand-cast pipe, SB-12-3, of manufacturer A was the only bell-end specimen on which deflection readings were obtained with the load applied at the center of the bearing block rather than at the center of the length of the pipe. Comment has already been made regarding the effect of this eccentric load application on the supporting strength and, as is to be expected, its influence on deflections is apparent. Comparing the deflections of specimen SB-12-3 under a load of either 3,000 or 4,000 pounds it will be noted that the deflection of the spigot end is about 56 percent greater than the deflection of the corresponding plain-end specimen, SP-12-1. For the 16 - and 20 -inch pipe of manufacturer A and the 18 -inch pipe of manufacturer B, all of which were tested with the load applied at the center of length of the pipe, the deflections of the spigot end of the bell-end pipe are about the same as the deflections of the corresponding pipes with plain ends. Other things being equal, deflections are directly proportional to loads and therefore it is to be expected, as has already been shown to have been the case, that an eccentricity of load application which causes the spigot end of a bell-end pipe to deflect much more than a plain-end pipe of the same metal and dimensions under symmetrical loading, will cause the bell-end pipe to fail at a lower load than the pipe with plain ends.
The data of table 6 and the curves of figure 8, which are all concave downward, show that the deflections increased at a somewhat greater rate than the corresponding loads.

A comparison of the average deflections of bell-end pipe with those of pipe with plain ends shows that in all cases, the presence of the bell resulted in a greater stiffness of pipe. However, only short lengths of pipe were tested. The increased stiffness is not always the same and this may be attributed to differences in the bells themselves.
Comparison of deflections of different types of pipe of the same size shows some differences in flexibility but it should not be concluded that these differences are necessarily inherent in the type itself. The type may have a considerable influence, as in the case of the spiral-corrugated pipe, which naturally is much stiffer than a smooth pipe of the same shell thickness, but the details of design are also of great importance. In general, pipe of the larger sizes show a greater flexibility than those of smaller size but this need not necessarily be the case. It should be remembered that deflection of a smooth pipe under a given load is dependent on three variables-diameter, shell thickness, and the modulus of elasticity of the metal.
The vertical deflection of smooth pipe with plain ends in the 2-edge bearing test ${ }^{3}$ is given by the equation ${ }^{4}-$

$$
\begin{equation*}
\Delta y=0.15 \frac{P r^{3}}{\overline{E I}} \tag{2}
\end{equation*}
$$

where
$\Delta y=$ vertical deflection, in inches,
$P=$ load, in pounds,
$r=$ radius of center line of shell, in inches,
$E=$ modulus of elasticity, in pounds per square inch,
$I=$ moment of inertia of a longitudinal element of the shell, in inches ${ }^{4}$.

[^3]

Figure 8.-Typical Load-Deflection Curves. An Asterisk Following the Serial Number Indicates Deflections Are Averages of Measurements at Each End of Pipe.

This equation is applicable to pipe of constant section and constant modulus of elasticity. Cast-iron pipes, due to unavoidable inaccuracies in manufacture, are not accurately uniform in cross section and the modulus of elasticity of cast iron is not a constant. However, the formula is useful as a basis of comparison and, as has been pointed out by Talbot, may be used somewhat empirically.

By making suitable substitutions, equation 1 may be reduced to the form-

$$
\Delta y=\frac{0.225 P\left(1+\frac{t}{d}\right)^{3}}{E b\left(\frac{t}{d}\right)^{3}}
$$

where
$t=$ shell thickness, in inches,
$d=$ inside diameter of pipe, in inches,
$b=$ length
$b=$ length of pipe, in inches.
For convenience equation 2 may be written-

$$
\begin{equation*}
\Delta y=\frac{0.225 P}{E b} \tag{3}
\end{equation*}
$$

where

$$
K=\frac{\left(1+\frac{t}{d}\right)^{3}}{\left(\frac{t}{d}\right)^{3}}
$$

Thus, for constant value of load, modulus of elasticity, and length of pipe, there is a straight-line relationship between deflections"and values of $K$.

Values of $\frac{t}{d}$ and $K$ for the smooth pipe with plain ends are given in table 6 and, in figure 9 , these values of $K$ have been plotted against the corresponding observed deflections. The values of $t$ used in computing $K$ are the average thicknesses as measured along the crack in the pipe and given both in tables 1, 2, and 3 and tables 7, 8, and 9. Values of $d$ are the average inside diameters as given in tables 7,8 , and 9 . Since the pipe shells did not have a constant thickness and were not always exactly circular in cross section, these values of $t$ and $d$ are not necessarily the true values which should be used in computing deflections. However,
they are the best figures available and it is believed that there are no departures from true values of sufficient magnitude to introduce errors of consequence in this discussion. Therefore, the deviations of the plotted points from the straight-line relationships shown in figure 9 are due primarily to deviations of the moduli of elasticity from the average modulus at this particular load.


Figure 9.--Relationship Between Vertical Deflections in 3-Edge Bearing Test and Values of $K$ for Smooth Cast-Iron Pipe with Plain Ends Based on a Load of 3,000 Pounds per Linear Foot of Pipe.

The average straight-line relationships between vertical deflections and values of $K$, for the three groups of pipe, correspond to moduli of elasticity of $14,400,000$, $15,000,000$, and $19,300,000$ pounds per square inch, respectively, for the sand-cast pipe of manufacturer B, the sand-cast pipe of manufacturer A and the centrifugally cast pipe. This order of values of moduli is not in agreement with the order of values shown by the strip tests which will be described later. The average values of moduli of elasticity, as determined by tests on strips, are lowest for the sand-cast pipe of manufacturer A and highest for the centrifugally cast pipe.

While there is a fairly large difference between the average moduli of the sand-cast pipe and that of the centrifugally cast pipe, it is apparent that, for the smooth pipe included in this study, the magnitude of the vertical deflections under a given load in the 3-edge bearing test was influenced more by variations in the ratio of shell thickness to diameter than by variations in the modulus of elasticity of the metal.

## MODULUS OF RUPTURE OF PIPE STUDIED

The load capacity of cast-iron pipe in the 3 -edge bearing tests is influenced by the diameter of the pipe, the thickness of the shell, and the strength of the metal, and it is impossible to study the influence of any one of these variables without a knowledge of the other two. In any given case, the first two variables may be determined by measurement. As a measure of the third variable, the strength of the metal, the modulus of rupture, computed from the results of tests, is useful.
The 2-edge or "knife-edge" bearing test is the same as the 3 -edge bearing test except that in the former the lower bearing consists of a single strip instead of two strips as in the latter. Thus, in the 2-edge test the
specimen is loaded through the upper and lower elements which are in a vertical plane through the longitudinal axis of the pipe. It has been shown ${ }^{5}$ that in a thin elastic ring loaded in this manner the maximum moment occurs under the load and is given by the equation

$$
\begin{equation*}
M_{2}=\frac{P r}{\pi} \tag{4}
\end{equation*}
$$

where
$M_{2}=$ bending moment, in inch-pounds, $P=$ load, in pounds, $r=$ radius of center line of ring, in inches.
It has also been shown ${ }^{5}$ that, for a thin, elastic ring in the 3 -edge bearing test, the moment under the load is given by the equation--

$$
\begin{equation*}
M_{3}=\frac{P r}{2 \pi}\left(1+\sqrt{1-\frac{a^{2}}{r^{2}}}+\frac{a}{r} \alpha-\frac{a^{2}}{r^{2}}\right) \tag{5}
\end{equation*}
$$

where

$$
\begin{aligned}
& M_{3}=\text { bending moment in inch-pounds, } \\
& P=\text { load in pounds, } \\
& r=\text { radius of center line of ring in inches, } \\
& a=\text { one half the distance, between the lower } \\
& \text { bearing strips in inches, } \\
& \alpha=\text { angle, in radians, whose sine equals } \frac{a}{r} \text {. }
\end{aligned}
$$

Equation 4 gives calculated bending moments somewhat larger than those given by equation 5 but the difference is so slight as to be negligible for pipe having the dimensions of those which are under discussion. For example, for a pipe having an inside diameter of 12 inches and a shell thickness of one half inch, the moment for the 2 -edge bearing exceeds that for the 3 -edge bearing with lower bearings 1 inch apart, by less than 1 percent. The same is true for a pipe having an inside diameter of 48 inches, a shell thickness of 1 inch, and the lower bearings in the 3 -edge test spaced 4 inches apart. Since this is the case, it will be sufficiently accurate, and more convenient on account of its greater simplicity, to use the equation for the 2 -edge bearing test in calculating the modulus of rupture for pipe tested in the 3 -edge test.
The modulus of rupture may be calculated from the usual flexure formula

$$
\begin{equation*}
R=\frac{M c}{I} \tag{6}
\end{equation*}
$$

where
$R=$ modulus of rupture, or computed fiber stress in pounds per square inch,
$M=$ bending moment in inch-pounds,
$c=$ distance from neutral axis to extreme fiber in inches,
$I=$ moment of inertia of the section (longitudinal element of the shell), in inches ${ }^{4}$.
Combining equations 4 and 6 ,

$$
R=\frac{\operatorname{Prce}}{\pi I}
$$

[^4]Let
$d=$ inside diameter of pipe in inches,
$t=$ shell thickness in inches,
$b=$ length of pipe in inches.
Then

$$
R=\frac{0.955 P(d+t)}{b t^{2}}
$$

When
$b=12$ inches and $P=$ load in pounds per linear foot of pipe,

$$
R=\frac{.0796 P(d+t)}{t^{2}}
$$

The flexure formula, equation 6, is based on the assumptions that the modulus of elasticity is a constant and that the fiber stress is within the elastic limit of the material. For cast-iron at the breaking load these assumptions are not fulfilled and therefore the modulus of rupture, as given by equations 7 or 8 , is not the true stress in the outer fiber. However, as with other materials, the calculated modulus of rupture of cast-iron is a useful measure of the strength of the material at its ultimate load.

## DESIGN DATA PRESENTED

Values for the moduli of rupture of the smooth pipe with plain ends (described in tables 1, 2, and 3) have been calculated from equation 8 and the results are given in tables 7,8 , and 9 . These tables also give the average inside diameters of the pipe, which generally vary somewhat from the nominal diameters; and the maximum and minimum, as well as the average, thickness of shell at the break. In the computations, the average inside diameter was substituted for $d$ and the average shell thickness at the break for $t$.

Table 7.-Breaking load and moduli of rupture of smooth sandcast pipe with plain ends of manufacturer A

| Identification no. | Nomjnal diameter | $\begin{aligned} & \text { Aver- } \\ & \text { age } \\ & \text { inside } \\ & \text { diam- } \\ & \text { eter } \end{aligned}$ | Shell thickness at break |  |  | Breaking load | Modu- <br> lus of <br> rup- <br> ture | Average | Deviation from grand a verage |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Maximum | Mini- <br> mum | Average ${ }^{1}$ |  |  |  |  |
| SP-12-1 | $\begin{gathered} \text { Inches } \\ 12 \\ 12 \end{gathered}$ | Inches | Inches <br> 0.47 | Inches 0.44 | Inches$0.45$ | Lb. per foot | Lb. per sa. in. | 1.6. ner sq. in. | Per- <br> cent |
|  |  | 12.2 |  |  |  | 8,520 | Sq. 300 |  |  |
|  |  | 12. 2 | 46 | . 41 | . 44 | 7,750 | 40, 300 | 40, 800 | 7.8 |
|  | 12 | 12.2 | . 46 | . 41 | . 44 | 7,650 | 39,700 |  | 6.1 |
| SP-16-1 | 16 | 16.2 | . 58 | . 52 | . 55 | 8, 140 | 35, 900 |  | 4. 0 |
| , | 16 | 16. 2 | . 52 | . 48 | . 50 | 7,350 | 39, 100 | 37, 700 | 4.5 |
| , | 16 | 16. 2 | . 54 | . 49 | . 51 | 7, 440 | 38,000 |  | 1.6 |
| SP-20-1 | 20 | 20.5 | . 54 | . 52 | . 53 | 7,270 | 43,300 |  | 15.8 |
| $\frac{2}{3}$ | 20 | 20.5 | 52 | . 47 | . 50 | 6,550 | 43, 700 | 41, 400 | 16.8 |
| 3 | 20 | 20.5 | . 51 | . 50 | . 50 | 5,580 | 37,300 |  | . 3 |
| SP-24-1 | 24 | 24.5 | . 55 | . 53 | . 54 | 4, 800 | 32,800 |  | 12.3 |
|  | 24 | 24.5 | . 59 | . 53 | . 56 | 6, 040 | 38,400 | 38, 200 | 2.7 |
|  | 24 | 24.5 | . 57 | . 53 | . 55 | 6, 580 | 43, 400 |  | 16.0 |
| SP-30-1 | 30 | 30.2 | . 71 | . 65 | . 68 | 7,490 | 39, 500 |  | 6.4 |
| 2 | 30 | 30.2 | . 77 | . 72 | . 74 | 7,120 | 32,000 | 34, 400 | 14.4 |
| 3 | 30 | 30.1 | . 76 | . 71 | . 73 | 6,830 | 31,500 |  | 15.8 |
| SP-36-1 | 36 | 36.2 | . 85 | . 82 | . 84 | 8, 530 | 35, 600 |  | 4.8 |
| 3 | 36 | 36.0 | . 93 | . 88 | . 91 | 9,500 | 33, 700 | 34, 600 | 9.9 |
| $\therefore P-42-1$ | 42 | 42.0 | 1. 08 | 1.04 | 1.06 | 11, 980 | 36, 500 |  | 2.4 |
|  | 42 | 42.0 | 1. 01 | . 99 | 1. 00 | 10, 430 | 35, 700 | 37,700 | 4. 5 |
| $\theta$ | 42 | 42.1 | . 96 | . 92 | . 93 | 10, 320 | 40, 800 | 37, 700 | 9.1 |
| SP-18-1 | 48 | 48.4 | 1. 05 | 1. 00 | 1.02 | 8, 400 | 31, 800 |  | 15. 0 |
| 2 | 48 | 48.5 | 93 | . 87 | . 90 | 7,430 | 36, 100 | 33, 500 | 3.5 |
| 3 | 48 | 48.5 | 99 | 95 | . 97 | 7,820 | 32, 700 |  | 12.6 |
| Grand av |  |  |  |  |  |  | 37, 400 |  | 8.7 |

Table 8.-Breaking load and moduli of rupture of smooth sandcast pipe with plain ends of manufacturer $B$

| Identification no. | Nom- <br> inal <br> diam- <br> eter | Average inside diameter | Shell thickness at. break |  |  | Breaking load | Modulus of rupture | Average | Deviation from grand average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Maximum | Minimum | Average 1 |  |  |  |  |
|  |  |  |  |  |  | Lh. per foot | Lb. per sq. in. | $\begin{aligned} & \text { Lb. per } \\ & \text { sq. in. } \end{aligned}$ | Per- <br> cent |
| SP-12-1 | Inches 12 | $\begin{aligned} & \text { nches } \\ & 11.9 \end{aligned}$ | $0.59$ | $0.44$ | $0.51$ | $8,200$ | $31,100$ | $\text { sq. } \mathrm{mn} \text {. }$ | $9.3$ |
|  | 12 | 11.9 | . 50 | . 42 | . 46 | 6,900 | 32, 100 | 33, 500 | 6.4 |
| - 3 | 12 | 12.0 | 51 | . 44 | . 48 | 8,650 | 37, 300 |  | 8. 7 |
| SP-18-1 | 18 | 18.0 | . 55 | . 43 | . 48 | 4,280 | 27, 300 |  | 20.4 |
| 2 | 18 | 18.0 | . 47 | . 42 | . 44 | 4,870 | 36, 900 | 34, 900 | 7.6 |
| , | 18 | 17.9 | . 52 | . 44 | . 47 | 6, 120 | 40,500 |  | 18.1 |
| SP-24-1 | 24 | 23.8 | . 63 | . 55 | . 60 | 5, 850 | 31,500 |  | 8. 2 |
| , | 24 | 24.0 | . 64 | . 57 | . 62 | 7,300 | 37, 200 | 35,400 | 8.5 |
|  | 24 | 24.0 | . 61 | . 60 | . 60 | 6, 890 | 37, 500 |  | 9.3 |
| -10-30-1 | 30 | 30.0 | . 75 | . 59 | . 70 | 6,780 | 33, 800 |  | 1.5 |
| 2 | 30 | 30.0 | . 70 | . 65 | . 68 | 6, 630 | 35, 000 | 33, 600 | 2. 0 |
| 3 | 30 | 30.0 | . 72 | . 59 | . 68 | 6, 090 | 32, 100 |  | 6. 4 |
| SP-3f-1 | 36 | 36.0 | 1. 03 | 88 | . 95 | 10,590 | $34,500$ |  | . 6 |
| , | 36 | 36.0 | . 99 | . 82 | . 94 | 10, 170 | $33,800$ | 134,200 | 1.5 |
| Grand av |  |  |  |  |  |  | 34,300 |  | 7.7 |

1 Average of thickness at 10 equally spaced points along the crack.
TABLe 9.--Breaking load and moduli of rupture of smooth centrifugally cast pipe with plain ends

| Identification no. | Nom- <br> inal <br> diam- <br> eter | Average inside diameter | Shell thickness at break |  |  | Breaking load | Modu: lus of rupture | Average | Deviation from grand average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Maximum | Minimum | A verage : |  |  |  |  |
|  | Inches | Inches | Inches | Inches | Inches | L.6. per foot | $\begin{aligned} & \text { Lb. per } \\ & \text { sq.in. } \end{aligned}$ | 1.b. per sq.in. | Percent |
| CP-12-1 | 12 | 12.4 | 0. 43 | 0.42 | 0. 42 | 8,650 | 50,000 |  |  |
| 2 | 12 | 12.4 | . 42 | . 40 | . 41 | 9,020 | 54, 700 | 52,800 | 4. 6 |
| 3 | 12 | 12.4 | 43 | 41 | . 42 | 9,270 | 53, 600 |  | 2.5 |
| CP-16-1 | 16 | 16.4 | . 53 | . 50 | . 51 | 10,770 | 55, 700 |  | 6.5 |
| , | 16 | 16. 2 | . 50 | . 49 | . 49 | 10, 800 | 59,700 | 55, 600 | 14.1 |
| 3 | 16 | 16.0 | . 65 | . 52 | . 58 | 13, 130 | 51, 500 |  | 1. 5 |
| CP-20-1 | 20 | 20.2 | . 63 | . 62 | . 63 | 10,710 | 44,700 |  | 14.5 |
|  | 20 | 20. 2 | . 68 | . 63 | . 65 | 12,480 | 49,000 | 48, 600 | 6.3 |
|  | 20 | 20. 2 | . 61 | . 57 | . 59 | 10,960 | 52, 100 |  | 0.4 |
| Grand a |  |  |  |  |  |  | 52,300 |  | 6.1 |

${ }^{1}$ Average of thickness at 10 equally spaced points along the crack.
In comparing the average moduli of rupture of the three groups of specimens shown in these tables, the relatively high modulus of the centrifugally cast pipe is noteworthy. The pipe of this group have an average modulus of rupture of 52,300 pounds per square inch as compared with 37,400 pounds per square inch for the sand-cast pipe of manufacturer A and 34,300 pounds per square inch for the sand-cast pipe of manufacturer B. These results, as well as those of the strip tests to be described later, show that the centrifugally cast metal in these specimens is unquestionably of materially higher strength than the metal in the specimens which were cast in sand molds in accordance with common foundry practice.

The consistency of the values of modulus of rupture developed by individual specimens in each of the three groups is considered to be reasonably good, the average deviations being 8.7 percent, 7.7 percent, and 6.1 percent, respectively, for the sand-cast pipe of manufacturer A, the sand-cast pipe of manufacturer B, and the centrifugally cast pipe. The relatively low average deviation for the centrifugally cast pipe may be indicative of a more uniform product but this figure is established by fewer specimens than in the other groups and the maximum deviations for irdividual specimens of centrifugally cast pipe are not greatly lower than are those for individual specimens of the sand-cast pipe of manufacturer A .

It is important to note that, in spite of the reasonably low average deviations, the calculated moduli of rupture of individual specimens vary through a rather wide range in all three groups. For the sand-cast pipe of manufacturer A the modulus of rupture varies from a minimum value of 31,500 pounds per square inch to a maximum of 43,700 pounds per square inch and the maximum deviation from the average is 16.8 percent. The variation for the sand-cast pipe of manufacture $B$ is from 27,300 to 40,500 pounds per square inch with a maximum deviation of 20.4 percent, while for the centrifugally cast pipe the range is from 44,700 to 59 ,700 pounds per square inch with a maximum deviation of 14.5 percent.

The moduli of the sand-cast pipe of manufacturer A and of the centrifugally cast pipe show a general trend, though not a very marked or consistent one, toward lower values with increasing thicknesses of shell. The moduli developed by the sand-cast pipe of manufacturer B appear to be independent of shell thickness.

A knowledge of the modulus of rupture of cast-iron pipe, which may be expected in any particular case, is useful in designing pipe to resist a given load in the 3 -edge bearing test, or in predicting the approximate load which pipe of a given thickness and known quality of metal will support.

The strength of pipe in the 3-edge test is commonly expressed in pounds per linear foot of pipe per foot of pipe diameter. Thus, pipe is said to have a strength of $2,000 D$ pounds per linear foot, $D$ being the nominal inside diameter of the pipe in feet. In this connection it is convenient to transpose equation 8 into another form.

In this equation-
$P=$ load in pounds per linear foot of pipe,
$d=$ inside diameter of pipe, in inches,
Let $L=$ load in pounds per linear foot of pipe per foot of pipe diameter.
Then $P=\frac{L d}{12}$
Substituting in equation 8 ,

$$
R=\frac{.0796 L d(d+t)}{12 t^{2}}
$$

and

$$
\begin{equation*}
L=\frac{12 R t^{2}}{.0796 d(d+t)}=\frac{12 R t^{t^{2}}}{.0796\left(1+\frac{t}{d}\right)} \tag{9}
\end{equation*}
$$

Thus, for any given value of load, $L$, and modulus of rupture, $R$, the ratio of shell thickness to diameter $\frac{t}{d}$ is a constant.

The curves of figure 10 are based on calculations made with equation 9 and may be used to determine the shell thickness of smooth cast-iron pipe for any required strength and assumed modulus of rupture, or to predict the approximate strength of pipe when the ratio, $\frac{t}{d}$, and the approximate modulus of rupture is known.

In designing pipe for strength by the use of equation 9 consideration should be given, in the selection of the value of $R$ to be used, to the range in values of modulus of rupture which may be expected in pipe manufactured to meet the design requirements. Also, some allowance in shell thickness should be made as a safeguard


Figure 10.-Theoretical Relation Between Ultimate Load in the 3-Edge Bearing Test and the Ratio of Shell Thickness to Inside Diameter for Smooth CastIron Pipe with Plain Ends.
against unavoidable inaccuracies in the manufacture of the pipe. An arbitrary increase in the theoretical thickness given by equation 9 , of not less than 10 percent is suggested.

## BENDING TESTS MADE ON STRIPS CUT FROM PIPE

Some specifications for cast-iron pipe, notably those of the Federal Government, require bending tests on small machined strips cut from sample pipe, and provide limiting values for the modulus of rupture of such strips and for the secant modulus of elasticity at the breaking load.

For example, the following requirements are quoted from Federal Specification WW-P-421 for Cast-Iron Water Pipe (Bell and Spigot):

F-4a. From each 300 lengths of pipe, or fraction thereof, of each size in the contract or order, one length of pipe shall be selected by the inspector before coating. From each sample pipe there shall be cut and machined one test strip 12 inches long, 0.50 inch deep, and the full thickness of the shell in width. This shall be tested as a beam (with machined surfaces top and bottom) on supports 10 inches apart with load applied at two points $3 \frac{1}{3}$ inches from the supports. The strip shall be accurately calipered at point of rupture and stress calculated by the formula

$$
S=\frac{P L c}{6 I}, \text { or for the above specimen } S=\frac{40 P}{b}
$$

F-4b. The secant modulus of elasticity at the breaking load shall be calculated by the formula

$$
H=\frac{23 P L^{3}}{1296 I y} \text {, or for the above specimen } E=S^{\frac{42.6}{y}}
$$

In these formulas,
$S=$ modulus of rupture,
$E=$ modulus of elasticity,
$P=$ total load,
$L=$ length of span,
$c=$ distance to extreme fiber,
$I=$ moment of inertia,
$b=$ width of specimen (thickness of pipe),
$d=$ depth of specimen,
$y=$ center deflection at load $\mu$.
It has been suggested that the modulus of rupture developed by these small test specimens might serve as an index of the modulus of rupture developed by


Figure 11.-Apparatus for Testing Small Strips of Metal Cut from Cast-Iron Pipe.
the specimens of pipe from which the strips are cut in the 3 -edge bearing test. The advantages to be gained by testing small strips of metal rather than fullsize specimens of pipe, both from the standpoint of convenience and economy, are manifest. In order to determine the suitability of the strip test as a measure of the supporting strength of pipe, a complete series of tests was made on strips cut from all the smooth pipe with plain ends which are listed in tables 7,8 , and 9 .

The strips were taken from the pipe which had been broken in the strength tests and were machined and tested in accordance with the specifications quoted above. A 20,000 -pound universal testing machine, converted to 2,000 -pound capacity for these tests, was used for applying the loads, the moving head being operated at an idle crosshead speed of 0.03 inch per minute.

The loads were applied to the strips at the third points through a system of cylindrical rollers and the specimen was supported by blocks with line-bearings which in turn were supported by a cylindrical bearing at one end and a spherical bearing at the other. A view of the testing apparatus is shown in figure 11.

The cross-sectional dimensions of the specimen at the point of rupture were determined by measurements with micrometer calipers. The modulus of rupture was computed from these dimensions and the load at failure. The pitch coating and any sand adhering to the surface of the metal was removed from the strips by grinding before they were tested.
The deflections of each strip at the center of span, for increments of load up to failure, were measured with a micrometer dial reading to 0.001 inch. The
deflection data were used to compute the tangent modulus of elasticity at the origin and the secant modulus of elasticity at failure.
The most convenient location in the broken pipe from which to obtain material for the strips was near the crack which had resulted in the failure of the pipe in the loading test. Since the metal in this area had been subjected to high stress it was necessary to make a preliminary investigation to determine if the physical characteristics of the metal had been materially altered by the stress to which it had been subjected. In this connection it should be noted that the direction of bending in the tests of the pipe was at right angles to that in the bending tests on the strips.

For the preliminary investigation, 3 strips were cut from each of 5 locations in the half circumference of the shell of one of the 48 -inch pipes with plain ends of manufacturer A (specimen SP-48-1). The strips were taken from the top (about 2 inches from the crack) and bottom of the shell, from a location on the horizontal axis through the center line and from points midway between this and the top and bottom. Thus there were specimens from two areas of maximum positive bending moment, one area of maximum negative moment, and two areas where the bending moment was very small.

The moduli of elasticity and of rupture calculated from the results of flexure tests on these strips are given in table 10. The results indicated that three strips, one from each of three locations, were defective and the values for these were not included in the calculations of average values. The individual values, exclusive of those of the defective strips, are quite con-


Figure 12.- Typical Ladad)fflection Curves of Strips from Smooth ('ast-Iron Pife with Piatn Ende.


Figure 13.-Typical Stress-Deflection Curves of Strips from Smooth Cast-Iron Pipe with Plain Ends.
sistent and the average values show no significant differences between strips taken from areas of high stress and those taken from areas of low stress. Table 10 shows that none of the defective strips were taken near the crack nor at the bottom of the pipe, the two positions of greatest bending moment. Therefore, it was concluded that the test strips from the other pipe might safely be taken from the vicinity of the crack which had developed under the loading test, and this was done.

## results of strip tests discussed

The results obtained in the strip tests are given in tables 11,12 , and 13, and typical load-deflection and stress-deflection curves are shown in figures 12 and 13.

In general, 3 strips from each pipe specimen were tested but in a number of cases, where flaws were observed, additional specimens were machined and tested. In most cases flaws in the metal could not be detected by visual examination before the strips had been broken and in numerous cases the flaws

Table 10.-Tests on strips from five positions in one 48 -inch pipe
[Modulus of rupture of pipe $-31,800$ pounds per square inch]

| Location of strips in pipe | Modulus of elasticity |  | Modulus of rup. ture |
| :---: | :---: | :---: | :---: |
|  | Origin | Failure |  |
| Top. | $\begin{aligned} & \text { Million } \\ & \text { lb. per } \\ & \text { sq.in. } \\ & 11.50 \\ & 10.35 \\ & 10.85 \end{aligned}$ | Million 1b. per <br> sq. in. $\begin{aligned} & \text { 4. } 60 \\ & \text { 4. } 65 \\ & \text { 4. } 79 \end{aligned}$ | $\begin{aligned} & \text { Lb. per } \\ & \text { sq.in. } \\ & 33,100 \\ & 32,500 \\ & 33,300 \end{aligned}$ |
| A verage... | 10. 90 | 4.68 | 33, 000 |
| $45^{\circ}$ from top... | $\begin{aligned} & 12.38 \\ & 11.85 \\ & 10.93 \end{aligned}$ | $\begin{aligned} & 5.02 \\ & 4.89 \\ & 6.17 \end{aligned}$ | $\begin{array}{r} 32,300 \\ 31,900 \\ 119,600 \end{array}$ |
| Average.. | 12. 12 | 4.96 | 32, 100 |
| $90^{\circ}$ from top. | $\begin{array}{r} 10.67 \\ 8.64 \\ 8.51 \end{array}$ | $\begin{aligned} & \text { 4. } 75 \\ & 5.97 \\ & 4.57 \end{aligned}$ | $\begin{array}{r} 33,600 \\ 122,400 \\ 31,500 \end{array}$ |
| A verage | 9. 59 | 4.66 | 32,600 |
| $45^{\circ}$ from bottom.. | $\begin{aligned} & 11.60 \\ & 11.20 \\ & 11.22 \end{aligned}$ | $\begin{aligned} & 6.07 \\ & 4.77 \\ & 4.84 \end{aligned}$ | $\begin{array}{r} 126,200 \\ 31,900 \\ 32,900 \end{array}$ |
| A verage... | 11.21 | 4.80 | 32,400 |
| Boitom. | $\begin{aligned} & 12.50 \\ & 12.46 \\ & 12.61 \end{aligned}$ | $\begin{aligned} & \hline 4.80 \\ & 4.93 \\ & 4.88 \end{aligned}$ | $\begin{aligned} & 32,800 \\ & 33,200 \\ & 34,000 \end{aligned}$ |
| Average....... | 12.52 | 4.87 | 33,300 |
| Grand average | 11.34 | 4. 79 | 32, 800 |

${ }^{1}$ Values for this strip excluded from averages.
which were observed had no apparent influence on the strength of the metal. For instance, 2 of the 3 strips from pipe SP-20-2 (table 11) had flaws and yet the modulus of rupture of both of these strips is higher than that of the strip in which no flaw was detected.

The test results for all strips, whether defective or not, are included in the tables and all results have been
used in computing average values except in the case of the average values of the ratio of modulus of rupture of strips to modulus of rupture of pipe (column 11, table 11, columns 11 and 20, table 12, and column 11, table 13). The following explanation is given for this procedure which is at variance with that usually followed in experimental work of this nature.
The strip test has been proposed as a specification requirement to replace, at least to some extent, the more cumbersome and more expensive 3 -edge bearing test on full-size specimens of pipe. If this is to be done, the strength developed by the strips should be indicative of the modulus of rupture of the pipe as determined in the 3 -edge test. A study of the data shows that flaws in the strips in some cases resulted in a material reduction of the modulus of rupture and in other cases did not. The data also show that strips with flaws and of low strength were sometimes obtained from pipe of more than average strength and, conversely, that strips of more than average strength were sometimes obtained from pipe of relatively low strength. It appears that, in routine testing to determine compliance with specifications, low strength due to flaws in strips would not necessarily be indicative of low-strength pipe. It is felt that, in the study of the suitability of the strip test for the proposed purpose, the test values of all specimens are of equal importance in arriving at conclusions.

As has been stated, the surfaces of the strips were ground to remove the coating of pitch and any adhering sand before testing. In the case of the sand-cast pipe of manufacturer A and the centrifugally cast pipe this did not result in appreciable reduction in the breadth of the specimen. However, the surfaces of the sandcast pipe of manufacturer B contained a considerable amount of embedded sand and the removal of this by grinding reduced the breadth of the specimens by varying amounts, frequently as much as several hundredths

Table 11.-Results of bending tests on strips from smooth sand-cast pipe with plain ends, manufacturer $A$

| Identification no. | Modulus of elasticity of strips |  |  |  | Modulus of rupture of strips | $\begin{aligned} & \text { A ver- } \\ & \text { age } \end{aligned}$ | Deviation from grand average | $\begin{aligned} & \text { Modu- } \\ & \text { lus of } \\ & \text { rup- } \\ & \text { ture of } \\ & \text { pipe } \end{aligned}$ | Ratio of modulus of rupture of strips to modulus of rupture of pipe |  | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | At origin | A verage | At failure | A verage |  |  |  |  |  |  |  |
| 1 | $\because$ | 3 | 4 | 5 | 6 | 7 | 8 | 3 | 10 | 11 |  |
| SP-12-1. | Million lb. per sq. in. 13. 37 13. 94 <br> 13. 01 | Million lb. per sq. in. 13. 44 | Million 16 . per sq. in. 9.13 9.22 8. 24 | Million lb. per $8 q . \mathrm{in}$. 8.86 | $\begin{aligned} & \text { Lb. per } \\ & \text { sq. in. } \\ & 35,100 \\ & 36,500 \\ & 38,300 \end{aligned}$ | $\begin{aligned} & \text { Lb. per } \\ & \text { sq. in. } \\ & 36,600 \end{aligned}$ | Percent 2. 8 1.1 6.1 | $\begin{aligned} & L b . \text { per } \\ & \text { sq.i.in. } \\ & 42,300 \end{aligned}$ | $\begin{array}{r} 0.83 \\ .86 \\ .91 \end{array}$ | $\begin{aligned} & \text { Aver- } \\ & \text { age } \\ & 0.87 \end{aligned}$ |  |
| 2. | $\begin{array}{r} 11.06 \\ 211.79 \\ \text { 12.63 } \end{array}$ | 11.83 | $\begin{aligned} & 8.44 \\ & 6.71 \\ & 6.71 \end{aligned}$ | 7.29 | $\begin{aligned} & 26,400 \\ & 36,400 \\ & 33,800 \end{aligned}$ | 32, 200 | $\begin{array}{r} 26.9 \\ .8 \\ 6.4 \end{array}$ | 40,300 | $\begin{array}{r} * .66 \\ .90 \\ .84 \end{array}$ | 1.87 | Flaw at break. |
| 3 | $\begin{aligned} & 11.26 \\ & 10.97 \\ & 11.30 \end{aligned}$ | 11. 18 | $\begin{aligned} & \text { 5. } 66 \\ & \text { 7. } 10 \\ & \text { 6. } 75 \end{aligned}$ | 6. 50 | $\begin{array}{r} 35,900 \\ \mid 31,500 \\ \mid 36,300 \end{array}$ | 34, 600 | $\begin{array}{r} .6 \\ 12.7 \\ .6 \end{array}$ | 39,700 | $\begin{array}{r} .90 \\ * .79 \\ . \quad .91 \end{array}$ | 1. 91 | Do. |
| A verage.. | 12.15 |  | 7. 55 |  | 34, 500 |  |  | 40,800 | . 85 | ${ }^{1 .} 88$ |  |
| SP-16-1.- | $\begin{aligned} & 12.76 \\ & 12.98 \\ & 12.56 \end{aligned}$ | 12. 77 | $\begin{aligned} & 6.92 \\ & 7.88 \\ & 7.03 \end{aligned}$ | 7. 27 | $\begin{aligned} & 41,900 \\ & 37,400 \\ & 40,000 \end{aligned}$ | 39,800 | $\begin{array}{r} 16.1 \\ 3.6 \\ 10.8 \end{array}$ | 35,900 | $\begin{aligned} & 1.17 \\ & \text { 1.04 } \\ & 1.11 \end{aligned}$ | 1.11 | Broke 0.05 inch outside middle third. |
| 2. | $\begin{aligned} & 11.88 \\ & 12.46 \\ & 13.96 \end{aligned}$ | 12.77 | $\begin{aligned} & 7.15 \\ & 7.33 \\ & 7.33 \end{aligned}$ | 7.27 | $\begin{aligned} & 38,600 \\ & 41,600 \\ & 40,400 \end{aligned}$ | 40,200 | $\begin{array}{r} 6.9 \\ 15.9 \\ 11.9 \end{array}$ | 39, 100 | $\begin{array}{r} .99 \\ 1.06 \\ 1.03 \end{array}$ | 1.03 | Broke 0.23 inch outside middle third. |
| 3. | $\begin{array}{r} 9.57 \\ 9.50 \\ 10.94 \end{array}$ | 10. 00 | $\begin{aligned} & \text { 6. } 20 \\ & \text { 5. } 94 \\ & \text { 6. } 15 \end{aligned}$ | 6. 10 | $\begin{aligned} & 35,800 \\ & 3,6,600 \\ & 39,800 \end{aligned}$ | 37, 700 | $\begin{array}{r} .8 \\ 4.2 \\ 10.2 \end{array}$ | 38,000 | $\begin{array}{r} .94 \\ .99 \\ 1.05 \end{array}$ | . 99 | Specimen warped. |
| A verage . . . . . | 11.85 |  | 6. 88 |  | 39, 200 |  |  | 37, 700 | 1.04 | 1.04 |  |

Table 11.-Results of bending tests on strips from smooth sand-cast pipe with plain ends, manufacturer. A-Continued


[^5]Table 12.-Results of bending tests on strips from smooth sand-cast pipe, plain ends, manufacturer $B$

${ }^{1}$ Values marked with asterisk (*) are omitted from this average.
of an inch. Moduli of rupture computed on the basis of the dimensions of the ground strips are undoubtedly more indicative of the strength of the metal itself than are similar values computed on the basis of the dimensions of the strips before grinding. However, moduli computed on the latter basis are more directly comparable to the moduli reported for the pipe specimens, since these were calculated on the basis of the gross thickness of shell, including embedded sand. Therefore, in table 12 which shows the results obtained on
strips from the pipe of manufacturer B, values of moduli of elasticity and rupture are reported for both unground and ground strips. The tests were made on the strips after grinding, and no tests were actually made on unground strips.

The moduli of elasticity and rupture reported for unground strips were obtained by using the loads and deflections of the ground strips and the dimensions of the strips in their original condition including the thickness of embedded sand. Since the grinding operation

Table 12.-Results of bending tests on strips from smooth sand-cast pipe, plain ends, manufacturer $B$ - Continued

${ }^{2}$ Deflection data for this strip shown in Figures 12 and 13.
unavoidably removed small amounts of surface metal, the strips in their original or unground condition probably would have supported somewhat greater loads than they did in the tests which were made. Therefore, the moduli reported for the unground strips in the first part of table 12 are probably somewhat lower than the true values but it is not believed that the error involved is large enough to be of any importance.

All average values given in tables 11, 12, and 13 are weighted averages and are based on all the test results, irrespective of defects in individual specimens, with the exception of the average values given in column 11 of table 11, columns 11 and 20 of table 12 and column 11 of table 13. In these columns are given the averages of the ratios of modulus of rupture of strips to modulus of rupture of pipe, and the moduli of strips manifestly

Table 13.-Results of bending tests on strips from smooth centrifugally cast pipe with plain ends


1 Values marked with asterisk (*) are omitted from the average.
${ }^{2}$ Deflection data for this strip shown in figures 12 and 13.
defective have been omitted in order to show the small effect on the grand averages of these columns as compared with the grand averages of the columns immediately preceding which are based on all test results. The omission of test results in the computation of these averages was based entirely on personal judgment. If the modulus of a strip was materially lower than the average of the other strips from that pipe, it was discarded; otherwise it was retained.

For each strip, two values of modulus of elasticity are reported; the secant modulus at failure and the tangent modulus at the origin. Of the two, the secant modulus is more suitable for use as a specification requirement on account of the greater ease and accuracy of its determination. The modulus at the origin is of some interest in showing the maximum value of modulus of elasticity which may be obtained in this test.

The average modulus of rupture of strips taken from the centrifugally-cast pipe is relatively high as was the case in the tests on full-size specimens. It may also be noted that in the tests of pipe the sand-cast pipe of manufacturer A developed a higher average modulus than the sand cast pipe of manufacturer B, while in the strip tests the reverse is true. The average modulus of 45,800 pounds per square inch for the strips of centrifugally cast metal may be compared with an average modulus of 38,200 pounds per square inch for the unground strips of sand-cast metal of manufacturer B and 36,100 pounds per square inch for the strips from
the sand-cast metal of manufacturer A. The ground strips from the sand-cast pipe of manufacturer B developed an average modulus of rupture of 40,600 pounds per square inch. The inclusion, in the computations, of the thickness of the embedded surface sand had the effect of reducing the average modulus about 6 percent to 38,200 pounds per square inch.
The consistency of the values of modulus of rupture developed by individual strips is indicated by the average deviations of 7.0 percent, 9.2 percent, and 11.8 percent, respectively, for the sand-cast metal of manufacturer A, the centrifugally cast metal and the unground strips of the sand-cast metal of manufacturer B. The relatively low average deviation of the moduli of rupture developed in the tests of centrifugally cast pipe may be thought to be indicative of a more uniform product, but this indication is not corroborated by the above results from tests on the metals themselves. The moduli of rupture of the ground strips (table 12) are somewhat more consistent than those of the unground strips. This is to be expected since the lowstrength material ground from the surface of the strips was not of uniform thickness.

## STRIP TESTS NOT A SATISFACTORYINDICATION OF PIPE STRENGTH

As in the case of the pipe specimens, the moduli of rupture of individual strips vary through a rather wide range. For the sand-cast strips of manufacturer A the modulus of rupture varies from a minimum of 21,000
pounds per square inch to a maximum of 43,800 pounds per square inch with a maximum deviation from the average of 41.8 percent. If the defective specimens are excluded, the range is from 32,400 to 43,800 pounds per square inch. For the unground sand-cast strips of manufacturer B, the variation is from 24,000 to 49,600 with a maximum deviation of 37.2 percent. Exclusive of defective specimens the range is from 32,700 to 49,600 pounds per square inch. Strips from the centrifugally cast pipe give a range in values of moduli of rupture from 30,400 to 54,000 pounds per square inch with a maximum deviation of 33.6 percent. Exclusive of specimens manifestly defective the range is from 40,600 to 54,000 pounds per square inch.

In the strip tests there is the same general, though far from consistent trend toward somewhat lower values of moduli of rupture with increasing thickness of metal as was the case in the pipe tests. However, the relationship is too vague to be of practical significance.

Both the tangent modulus of elasticity at origin and the secant modulus at failure, show the centrifugally cast metal to be considerably stiffer than the sand-cast metal. Average values for the tangent modulus at origin are $11,870,000$ pounds per square inch, $13,850,000$ pounds per square inch and $16,180,000$ pounds per square inch, respectively, for the sand-cast metals of manufacturer A , manufacturer B , and the centrifugally cast metal. Corresponding values for the secant modulus at failure are $6,240,000,8,390,000$, and $11,830,000$ pounds per square inch. Here, also, there is some indication of a general trend toward decreasing values with increasing thickness of metal, which appears to be somewhat more pronounced for the modulus at failure than for the modulus at origin, and more pronounced in the metal of manufacturer A and the centrifugally cast metal than in the metal of manufacturer B.

Possibly the most important data resulting from the strip tests are the calculated ratios of the modulus of rupture of each strip to the modulus of rupture of the pipe from which it was taken, and the average values of these ratios.

Including all strips, the values of the modulus ratio for the sand-cast pipe of manufacturer A range from 0.62 to 1.17 , with an average of 0.97 . The exclusion of badly defective strips changes the range to 0.83 to 1.17 and the average to 0.98 . The ratios for the centrifugally cast pipe range from 0.64 to 1.20 , with an average of 0.88 for all strips and, exclusive of defective specimens, an average of 0.90 with a range of 0.73 to 1.20 .
The modulus ratios for the unground strips from the sand-cast pipe of manufacturer B range from 0.64 to 1.78 , with an average of 1.11 , and the range for the ground strips is from 0.68 to 1.86 , with an average of 1.18. The exclusion of defective strips changes the ranges of individual values to 0.87 to 1.78 and 0.93 to 1.86 , respectively, with average values of 1.15 and 1.22 .

It will be observed that there is a considerable difference between the average values of the modulus ratios for the three groups of pipe. It will also be observed that the exclusion of the ratios for defective strips does not alter the average values materially and that there is the same general relationship between them irrespective of whether the defective strips are included or discarded.
It is, perhaps, to be expected that the average modulus ratio for the centrifugally cast pipe should differ
from those for the sand-cast pipe, since the physical characteristics of the metals themselves differ considerably. However, if the strength of strips is to be accepted as a measure of the strength of the pipe from which they are taken, a reasonably close agreement should exist between the modulus ratios for two sets of pipe cast in a similar manner and of metal of similar characteristics. This agreement does not exist for the sand-cast pipe, the average modulus ratios for all specimens being 0.97 for manufacturer A and 1.11 for the unground strips of manufacturer $B$.

It has been pointed out that (1) obviously defective strips may be obtained from pipe of more than average strength; (2) that strips of relatively high strength may be obtained from pipe of less than a verage strength; (3) that there is a wide range in the individual values of the modulus ratios; and (4) that there is lack of agreement between the average modulus ratios for two groups of pipe of the same general character. These facts lead to the conclusion that the results of tests on small strips cut from pipe are not acceptable indices of the strength which the pipe may be expected to develop in the 3 -edge bearing test.
USE OF TEST RESULTS IN PREPARATION OF SPECIFICATIONS
During the progress of the investigation which has been described, the results as they were obtained were made available from time to time to a committee of the American Society for Testing Materials which was engaged in the preparation of tentative specifications for cast-iron culvert pipe. These specifications, A.s. T.M. Designation: A142-32T, which have now been published as tentative standards of the society, are believed to be the first specifications for cast-iron culvert pipe in which the required shell thicknesses have been established on a rational basis.
These tentative specifications recognize three classes of pipe known as standard, heavy, and extra-heavy pipe for which the required minimum strengths in the 3 -edge bearing test are, respectively, $2,000 \mathrm{D}, 3,000 \mathrm{D}$, and $4,000 \mathrm{D}$ pounds per foot of laying length

The shell thicknesses for smooth pipe were calculated on the basis of equation 9 for a modulus of rupture of 30,000 pounds per square inch and the thicknesses so determined were arbitrarily increased by 10 percent. Table 14 gives the specified shell thicknesses and their derivation.

Table 14.-Shell thickness of smooth cast-iron culvert $i$ ipe as required by A.S.T.M. tentative standard specification, A1: $2-32 T$

| Nominal diameter of pipe (inches) | Standard pipe$(2,000 \mathrm{D})$ |  |  | Heavy pipe (3,000 D) |  |  | Extra-heavy pipe$(4,000 D)$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Theoretical thickness 1 | Theoretical thickness plus 10 percent | Speci- <br> fied <br> thick- <br> ness | Theoretical thickness ${ }^{1}$ | Theoretical thickness plus 10 percent | Specified thickness | Theoretical thickness ${ }^{1}$ | Theoretical thickness plus 10 percent | speci- <br> fier1 <br> thick- <br> ness |
|  | Inches | Inches | Inches | Inches | Inches | Inches | Inches | Inches | Inches |
| 12. | 0. 255 | 0. 281 | 0.37 | 0.313 | 0. 344 | 0.37 | 0. 362 | 0. 398 | 0.41). |
| 14 | 298 | . 328 | . 37 | . 365 | . 402 | . 40 | . 423 | . 465 | . 46 |
| 16 | . 340 | . 374 | . 40 | . 417 | . 459 | . 16 | . $4 \times 3$ | . 531 | 53 |
| 18 | . 383 | . 421 | . 42 | . 470 | . 517 | . 52 | . 543 | . 597 | tio |
| 20 | . 425 | . 468 | . 47 | . 522 | . 574 | . 57 | . 604 | . 664 | 856 |
| 24 | . 510 | . 561 | . 56 | . 626 | . 689 | . 69 | . 724 | . 796 | . 80. |
| 30 | . 638 | . 702 | . 70 | . 783 | . 861 | 86 | . 905 | . 996 | 1.00 |
| 36 | 765 | . 842 | . 84 | . 939 | 1. 033 | 1.03 | 1. 086 | 1. 195 | 1. 20 |
| 42 | 893 | . 982 | . 98 | 1. 096 | 1. 206 | 1. 20 | 1. 268 | 1. 395 | 1. 40 |
| 48 | 1. 020 | 1. 122 | 1. 12 | 1. 252 | 1.378 | 1.38 | 1. 449 | 1. 594 | 1. 60 |

quare inch.

It will be noted that the specified thicknesses of the $12-, 14-$, and 16 -inch standard pipe and of the 12 -inch hearr pipe are somewhat greater than the theoretical thicknesses increased by 10 percent. In these cases arbitrary increases were made in order that the required thickness of metal be not less than three eighths of an inch.

If the moduli of rupture obtained in the tests which have been reported may be considered generally representative of the values which would be obtained with any commercially available cast-iron culvert pipe, then the modulus of 30,000 pounds per square inch, which is the basis of design in the tentative specifications, may be considered somewhat conservative since it is somewhat lower than the average values which were obtained with sand-cast pipe. However, the modulus of one pipe tested was less than 30,000 pounds per square inch and the moduli of a considerable proportion were between 30,000 and 35,000 pounds per square inch. In any case, any conservatism in the matter of unit stress is balanced to some extent by the prorision of the specification which permits a maximum underrun in thickness of 15 percent.

## CONCLUSIONS

The following conclusions, based on the results obtained in this investigation, are presented:

1. In the 3 -edge bearing test for pipe with bell ends it is preferable to locate the point or center of load application, on the upper bearing block, at the center of pipe rather than at the center of length of bearing.
2. The design of cast-iron pipe to withstand the 3 edge bearing test may more safely be based on the results of tests on specimens with plain ends than on the results obtained on specimens with bell ends, due to the rariable and uncertain influence of the bell ends on the supporting strength.
3. The pipe included in this investigation which were centrifugally cast in metal contact molds were of considerably higher strength than the sand-cast pipe.
4. Spiral corrugated pipe and ribbed pipe, similar in all respects to those included in this investigation, may be expected to develop a strength in the 3 -edge bearing test of at least $2,000 D$ pounds per linear foot of laying length.
5. The magnitude of the vertical deflections of pipe under a given load in the 3 -edge bearing test is influenced by the type of design, the quality of the metal, and the details of design. For the smooth pipe included in this study the magnitude of these deflections was influenced more by variations in the ratio of shell thickness to diameter than by variations in the modulus of elasticity of the metal.
6. The modulus of rupture of small strips cut from a specimen of pipe is not a good index of the modulus of rupture which the pipe will develop in the 3 -edge bearing test.

## RECOMMENDATIONS

In addition to the above conclusions, it is desired to offer the following recommendations with respect to the design of smooth cast-iron pipe:

1. That the required minimum shell thickness be determined on a rational basis such as is provided by the theoretical equation (9) which has been presented.
2. That the selection of the modulus of rupture to be used in design be made on the basis of the modulus which may be expected in pipe manufactured to meet the design requirements.
3. That, as a safeguard against unavoidable inaccuracies in manufacture, the required nominal shell thickness be made greater than the theoretical thickness as determined by equation (9), by an arbitrary allowance of not less than 10 percent.

CURRENT STATUS OF U.S. PUBLIC WORKS ROAD CONSTRUCTION
LכV x 4 G
CLASS II-PROJECTS ON EXTENSIONS OF THE FEDERAL-AID HIGHWAY SYSTEM INTO AND THROUGH MUNICIPALITIES

| state | PUBLIC WORKS FUNDS ASSIGNED PROJECTS IN MUNICIPALITIES | COMPLETED |  |  |  | UNDER CONSTRUCTION |  |  |  |  | APPROVED FOR CONSTRUCTION |  | BALANCE OF PUBLIC available for NEW CLASS II PROJECTS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Teral cost | Public works funds | $\begin{aligned} & \text { Regular Fidederal } \\ & \text { aid } \end{aligned}$ | Mileage | Extimated total coot | Public works funds | Regular Federal aid allotted | Percentage completed | Mileage | Public worke funds allotted | Mileage |  |
| Alabama <br> Arizona <br> Arkansas | $\begin{aligned} & 2,092,533 \\ & 751,794 \\ & 1,687,084 \end{aligned}$ | \$ | \$ | \$ |  | $\begin{aligned} & 11.976 .30 \\ & 17.350 .27 \end{aligned}$ | $\begin{aligned} & \$ 0 \\ & \begin{array}{l} 11,976.30 \\ 9,963.18 \end{array} \end{aligned}$ | $7,387.09$ | $\begin{array}{r} 8.4 \\ 10.0 \end{array}$ | 1.0 .1 | $\begin{aligned} & \$ 119.619 .43 \\ & 207.534 .15 \end{aligned}$ | $\begin{aligned} & 6.2 \\ & 7.0 \end{aligned}$ | $\begin{aligned} & \$ .972,913.57 \\ & 1.769 .817 .70 \\ & 1,469.586 .67 \end{aligned}$ |
| California. Colorado Connecticut | 3.901. 839 <br> $1.718,633$ 802,407 |  |  |  |  | $\begin{aligned} & 125.384 .62 \\ & 105.469 .21 \\ & 369.505 .30 \end{aligned}$ | $\begin{aligned} & 112.319 .65 \\ & 105.49 .21 \\ & 369.505 .30 \end{aligned}$ |  | $\begin{array}{r} 3.6 \\ 62.6 \\ 1.9 \end{array}$ | $\begin{aligned} & 1.9 \\ & 3.0 \\ & 3.2 \\ & \hline \end{aligned}$ | 274.909 .28 <br> 132.295 .57 <br> 237.835.98 | $\begin{aligned} & 3.4 \\ & 3.1 \\ & 3.1 \end{aligned}$ | 3.514,610.07 <br> $1.480,868.22$ <br> 195.065.72 |
| Delaware <br> Florida <br> Georgia. | $\begin{aligned} & 454,772 \\ & 1,307,599 \\ & 2,724,620 \end{aligned}$ |  |  |  |  | $\begin{aligned} & 185,821.40 \\ & 139.270 .42 \end{aligned}$ | $\begin{array}{r} 185.821 .40 \\ 76.598 .73 \end{array}$ | 62,671.69 | $\begin{array}{r} 14.0 \\ 1.3 \end{array}$ | $\begin{aligned} & 2.0 \\ & 2.9 \end{aligned}$ | $\begin{array}{r} 13.542 .50 \\ 150.901 .19 \\ 12.325 .93 \end{array}$ | 2.8 .5 | $\begin{array}{r} 255.408 .10 \\ 1,080,459.08 \\ 2,712,294.07 \end{array}$ |
| Idaho <br> Illinois. <br> Indiana | $\begin{aligned} & 1,121,562 \\ & 6,877,199 \\ & 4,818,165 \end{aligned}$ |  |  |  |  | 39.947.35 | 39,947. 35 |  | 7.5 | 3.0 | $\begin{aligned} & 14,616.01 \\ & 24,444.60 \end{aligned}$ | $\begin{aligned} & .9 \\ & .4 \end{aligned}$ | $\begin{aligned} & 1,066.998 .64 \\ & 6,577199.00 \\ & 4,793.70 .40 \end{aligned}$ |
| Iowa <br> Kansas <br> Kentucky | $\begin{aligned} & 2,815,585 \\ & 2,522,40 \\ & 2,029,687 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 466,173.76 \\ 23.085 .32 \end{array}$ | $\begin{array}{r} 438.350 .00 \\ 23,085.32 \end{array}$ |  | $\begin{gathered} 37.0 \\ 8.7 \end{gathered}$ | 12.6 .4 | $\begin{array}{r} 477,500.00 \\ 73,830.32 \\ 31,123.23 \end{array}$ | $\begin{array}{r} 14.3 \\ 6.8 \\ 1.5 \\ \hline \end{array}$ | $\begin{aligned} & 1.899 .735 .00 \\ & 2,495.485 .36 \\ & 1.998 .563 .77 \end{aligned}$ |
| Louisiana <br> Maine <br> Maryland | $\begin{array}{r} 1,457.148 \\ 842,479 \\ 891.132 \end{array}$ |  |  |  |  | $\begin{array}{r} 224,717.31 \\ 410,082.40 \\ 16,788.76 \end{array}$ | 12,638.76 <br> $264,717.31$ 410.082 .40 12.638 .76 |  | $\begin{array}{r} 16.2 .2 \\ 21.2 \\ 7.9 \end{array}$ | 3.7 8.7 .6 | $\begin{aligned} & 141,679.31 \\ & 50,292.64 \end{aligned}$ | 7.4 2.1 | $\begin{array}{r} 1,050,751.38 \\ 382,103.96 \\ 878.493 .24 \end{array}$ |
| Massachusetts <br> Michigan <br> Minnesota $\qquad$ | $\begin{aligned} & 4,136,382 \\ & 4,45,769 \\ & 3,410,102 \end{aligned}$ |  |  |  |  | $\begin{aligned} & 385.758 .23 \\ & 273.520 .00 \\ & 972,113.85 \end{aligned}$ | $\begin{aligned} & 339.511 .37 \\ & 273.520 .00 \\ & 972,113.85 \end{aligned}$ | 40,000.00 | $\begin{aligned} & 15.6 \\ & 59.2 \\ & 35.9 \end{aligned}$ | $\begin{array}{r}5.1 \\ 5.9 \\ 48.3 \\ \hline 1.8\end{array}$ | $\begin{array}{r} 1,202,687.05 \\ 179.150 .00 \\ 457.127 .95 \end{array}$ | $\begin{array}{r}3.8 \\ 2.5 \\ 10.7 \\ \hline 1.7\end{array}$ | $\begin{aligned} & 2,594,183.58 \\ & 4,005,09.00 \\ & 1,980,860.20 \end{aligned}$ |
| Mississippi <br> Missouri <br> Montana | $\begin{aligned} & 1,7444.669 \\ & 3,045.077 \\ & 1,859.937 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 27,687.80 \\ 532,146.89 \\ 5,275.14 \\ 5 \end{array}$ | 15.228. 30 524,278.41 5, 275.14 | 12,459.50 | $\begin{array}{r} 7.4 .4 \\ 37.9 \end{array}$ | 1.8 4.0 .3 | $\begin{array}{r} 63,040.23 \\ 253,602.45 \\ 337,737.24 \end{array}$ | $\begin{array}{r} 2.2 \\ 4.8 \\ 10.8 \end{array}$ | $\begin{aligned} & 1,666,400.47 \\ & 2,267,196.14 \\ & 1,516,924.62 \end{aligned}$ |
| Nebraska. Nevada New Hampshire | $\begin{array}{r} 1.957 .240 \\ 500.045 \\ 477.460 \end{array}$ | 3.656.08 | 3.656 .08 |  | $1.3{ }^{\prime}$ | $\begin{array}{r} 448,863.57 \\ 50.303 .27 \\ 26.790 .69 \end{array}$ | 448.160 .17 <br> 50,304. 27 <br> 20,000.00 |  | $\begin{aligned} & 16.5 \\ & 77.5 \\ & 20.0 \end{aligned}$ | $\begin{array}{r} 11.5 \\ 1.2 \\ .3 \\ \hline \end{array}$ | $120,398.50$ $66,313.99$ | $\begin{aligned} & 4.8 \\ & 1.5 \\ & \hline \end{aligned}$ | $\begin{aligned} & 1.385,025.25 \\ & 449.746 .73 \\ & 391.146 .09 \end{aligned}$ |
| New Jersey <br> New Mexico <br> New York. | $\begin{aligned} & 3,217.442 \\ & 1,448,234 \\ & 1,837,665 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 671.930 .61 \\ 2,722,830.00 \\ \hline \end{array}$ | $\begin{array}{r} 671.930 .61 \\ 2.721 .530 .00 \\ \hline \end{array}$ |  | $\begin{array}{r} 16.8 \\ 6.1 \end{array}$ | 5.4 25.5 | $\begin{array}{r} 1,349,399.25 \\ 234.312 .35 \\ 2.936 .850 .00 \end{array}$ | 7.7 56.4 16.2 | $\begin{aligned} & 1,195,61.14 \\ & 1,213,921.65 \\ & 2,179,485.00 \end{aligned}$ |
| North Carolina North Dakota Ohio. $\qquad$ | $\begin{aligned} & 2,380.573 \\ & 1,451112 \\ & 4,645.378 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 81,177.36 \\ 15,572.15 \\ 806,110.00 \end{array}$ | $\begin{array}{r} 81.177 .36 \\ 15.57 .15 \\ 716.135 .00 \\ \hline \end{array}$ |  | $\begin{array}{r} 20.9 \\ 83.5 \\ 8.1 \end{array}$ | 4.5 4.8 9.0 | $\begin{array}{r} 34,177.12 \\ 146.818 .39 \\ 463.400 .00 \end{array}$ | 6.9 5.9 6.6 | $\begin{aligned} & 2,265,218.52 \\ & 1,288.72 .516 \\ & 3.465,843.00 \end{aligned}$ |
| Oklahoms Oregon Pennsylvania | $\begin{aligned} & 2,304,200 \\ & 1,526.724 \\ & 5,46,051 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 25.131 .78 \\ 190.977 .53 \\ 130.791 .78 \end{array}$ | $\begin{array}{r} 25,131.78 \\ 190,977.53 \\ 130,791.78 \end{array}$ |  | 67.6 | $\begin{aligned} & 1.7 \\ & 4.0 \\ & 3.5 \end{aligned}$ | $\begin{array}{r} 196,768.60 \\ 90,442.00 \\ 1,053.237 .00 \end{array}$ | $\begin{array}{r}4.9 \\ 2.9 \\ 2.6 \\ \hline\end{array}$ | 2,082,299.62 <br> 1.245.304.47 <br> 4,232,022.22 |
| Rhode Island South Carolina South Dakota | $\begin{array}{r} 499,677 \\ 1,364,791 \\ 1,502,870 \end{array}$ |  |  |  |  | $\begin{array}{r} 29.263 .72 \\ 119.000 .23 \end{array}$ | $28,858.71$ 119.000 .23 | 405.01 | 16.8 | 3.7 7.3 | 63.717 .66 140.903 .35 | 6.7 <br> 7.0 | $\begin{array}{r} 499,677.00 \\ 1,272,214.63 \\ 1,242.966 .42 \end{array}$ |
| $\begin{aligned} & \text { Tennessee. } \\ & \text { Texas.... } \\ & \text { Utah. } \end{aligned}$ | $2,123.155$ 6.061 .006 $1.048,677$ |  |  |  |  | $\begin{array}{r} 39.051 .81 \\ 97.45350 \\ 418.455 .50 \\ \hline \end{array}$ | $39,051.81$ $96,743.96$ 407.005 .45 |  | $\begin{array}{r} 7.7 \\ 3.1 \\ 40.5 \end{array}$ | 1.6 5.0 11.3 | $\begin{array}{r} 8.045 .84 \\ 427.855 .00 \\ 14.539 .25 \end{array}$ | .5 34.6 3.1 | $\begin{aligned} & 2.076 .075 .35 \\ & 5.536 .407 .04 \\ & 527.132 .30 \end{aligned}$ |
| Vermont <br> Virginia <br> Washington | $\begin{array}{r} 470.628 \\ 1.854 .189 \\ 1.877 .571 \end{array}$ |  |  |  |  | $\begin{array}{r} 67.791 .23 \\ 37.864 .96 \\ 103.208 .31 \end{array}$ | 66.772 .62 29.104 .47 103. 208. 31 | 8,760.49 | $\begin{array}{r} 4.5 \\ 17.2 \\ 20.3 \\ \hline \end{array}$ | 2.2 1.9 4.1 4 | $\begin{aligned} & 182.872 .63 \\ & 730.589 .25 \\ & 206.258 .11 \end{aligned}$ | 5.8 <br> 7.2 <br> 4.3 | $\begin{array}{r} 220,982.75 \\ 1,094,495.28 \\ 1,568.104 .58 \end{array}$ |
| West Virginia <br> Wisconsin <br> Wyoming | $\begin{aligned} & 1,342,270 \\ & 2,431,220 \\ & 1,125,332 \end{aligned}$ |  |  |  |  | $\begin{array}{r} 39.929 .76 \\ 709.629 .31 \\ 199.583 .12 \\ \hline \end{array}$ | $\begin{array}{r} 39.929 .76 \\ 709,629.31 \\ 179.083 .12 \end{array}$ |  | $\begin{array}{r} 35.1 \\ 29.3 \\ 2.2 \end{array}$ | 1.4 19.8 8.9 | 142,263.00 <br> 40,628. 77 | $\begin{aligned} & 2.2 \\ & 2.5 \\ & \hline \end{aligned}$ | 1,160,077.24 <br> 1.721.590.69 905.620 .11 |
| District of Columbia Hawaii | 1,151,081 |  |  |  |  | 197.493.65 | 197.493 .65 |  | 65.8 | 1.1 | 809,275.00 | 3.5 | 144.312 .35 |
| TOTALS | 113,515.642 | 3,656.08 | 3.656.08 |  | 1.3 | 11.580.989.12 | 11,277.994.03 | 131.683 .78 | 18.5 | 241.2 | 14,015,360.12 | 254.2 | 88,218,631.77 |





[^0]:    APPARATUS FOR TESTING CAST-IRON CULVERT PIPE

[^1]:    ${ }^{1}$ Acknowledgment is made to the United States Pipe and Foundry Co., the American Casting Co. and the Alabama Pipe Co. for the specimens of culvert pipe which were used in these tests.

[^2]:    ${ }^{2}$ Tests of Cast-Iron and Reinforced Concrete Culvert Pipe, by Arthur N. Talbot.

[^3]:    ${ }^{3}$ As will be shown in the discussion of modulus of rupture of pipe, this test may be considered, for all practical purposes, to be the same as the 3 -edge bearing test. \& Tests of Cast-Iron and Reinforced Conerete Culvert Pipe, by Arthur N. Talbot, Bulletin No. 22, University of Illinois.

[^4]:    5 Tests of Cast-Iron and Reinforced Concrete Culvert Pipe, by Arthur N. Talbot, Bulletin No. 22, University of Illinois. Experimental and Mathematical Analyses of Drain Tile Testing and New Test Bearing, by Dalton G. Miller and Josenh A. Wise, Technical Bulletin 52, University of Minnesota Agricultural Experiment Station.

[^5]:    ${ }^{1}$ Values marked with asterisk (*) omitted from this average.
    2 Deflection data for this strip shown in figs. 12 and 13.

